

Modelling the secular evolution of the Milky Way's disc

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with Vasily Belokurov, N. Wyn Evans, Jason L. Sanders and collaborators

Observational Constraints of Radial Migration in the Galactic Disk Driven by the Slowing Bar

HanYuan Zhang¹, Vasily Belokurov¹, N. Wyn Evans¹, Jason L. Sanders², Yuxi(Lucy) Lu^{3,4}, Chengye Cao⁵, GyuChul Myeong¹, Adam M. Dillamore², Sarah G. Kane¹, and Zhao-Yu Li^{5,6}

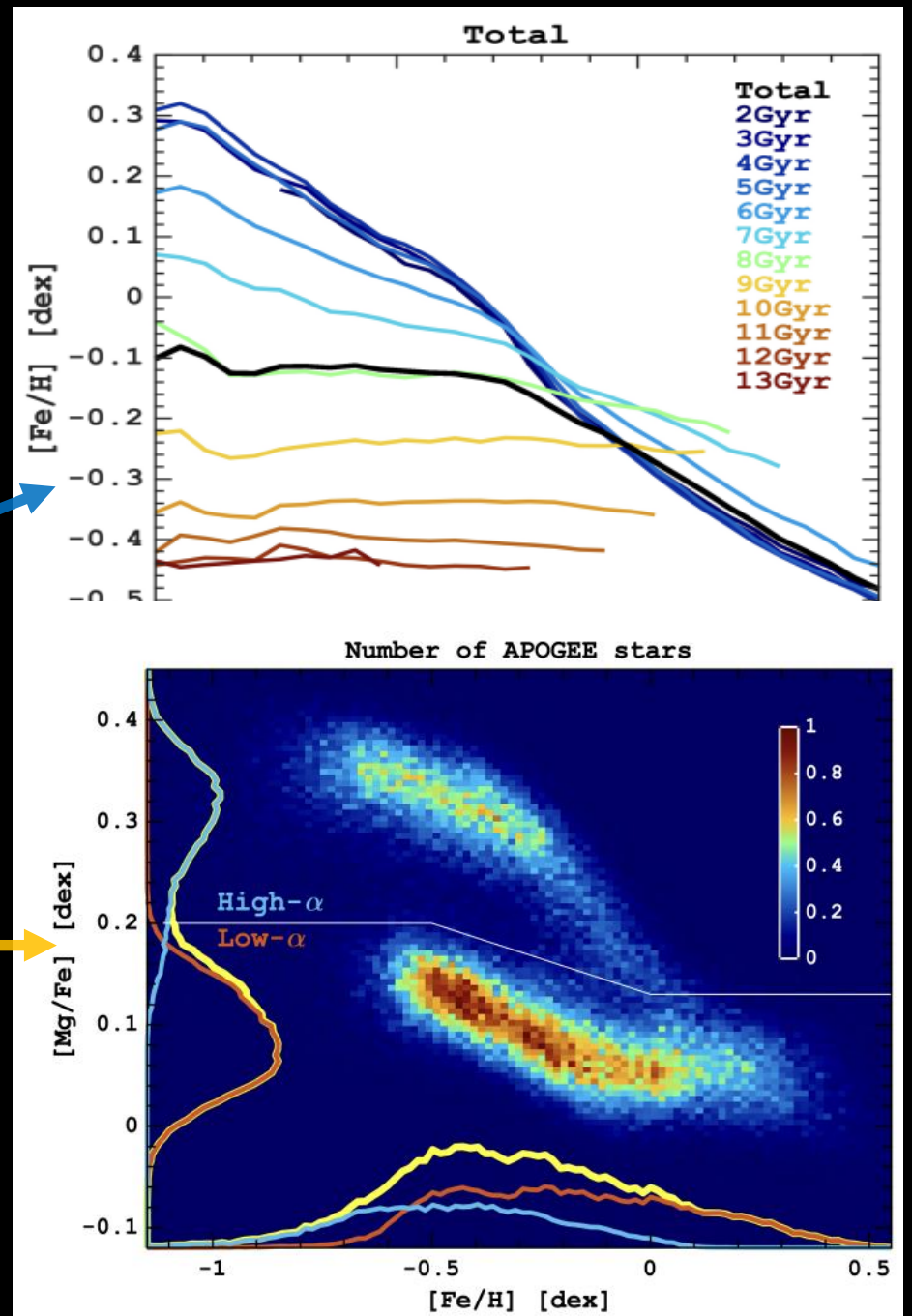
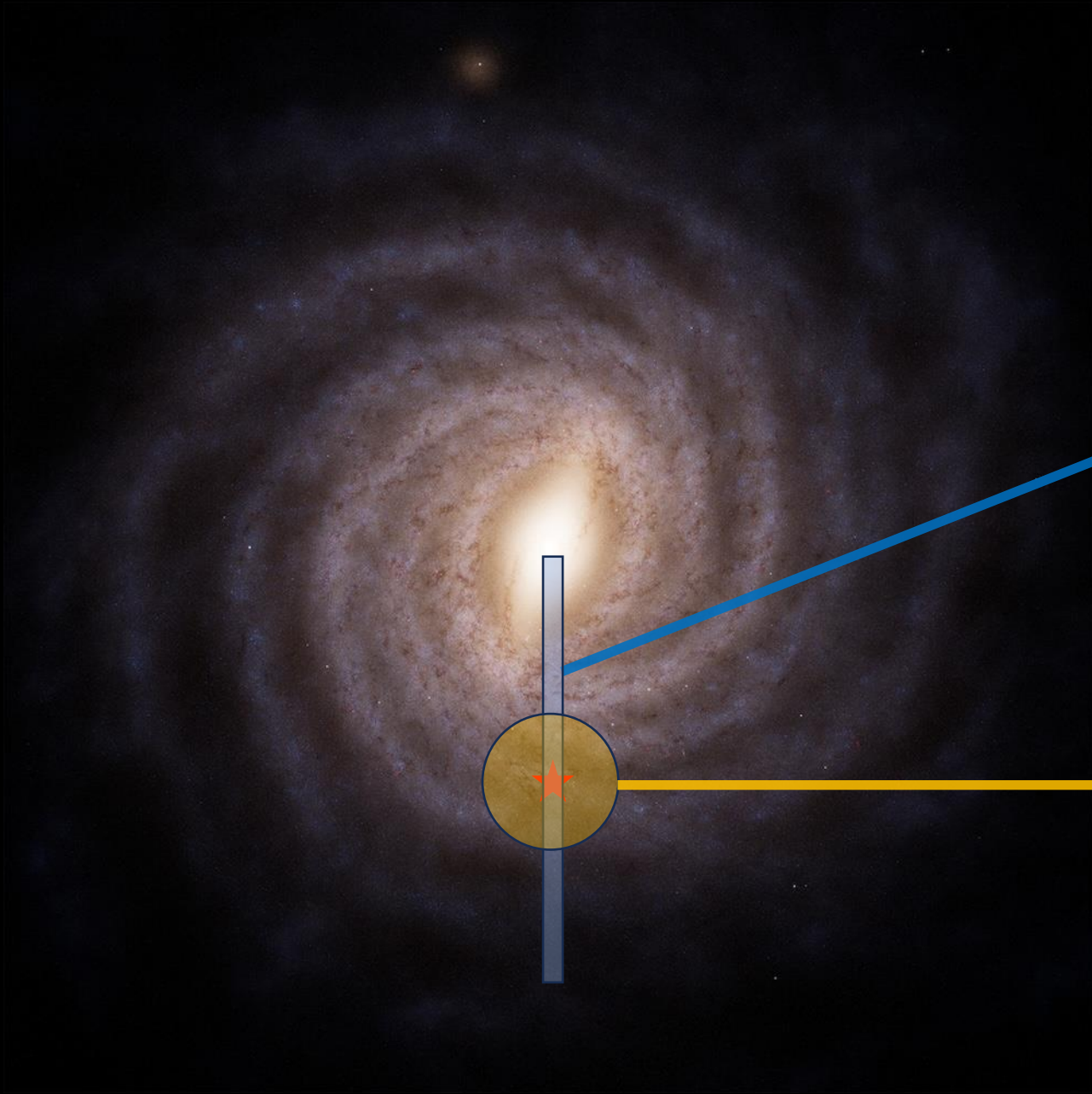
Orbital migration and heating history of the Galactic disc: a transition between the bimodal discs

HanYuan Zhāng,^{1*} Vasily Belokurov,¹ Jason L. Sanders,² N. Wyn Evans,¹ David Chemaly,¹ Daisuke Kawata,³ Natsuki Funakoshi,³ Neige Frankel,^{4,5} Sarah G. Kane,¹ and Sergey E. Koposov^{6,1}

Enhanced rates of stellar radial migration in gas-rich discs at high redshift

HanYuan Zhāng,^{1*} Thor Tepper-García,² Vasily Belokurov,¹ N. Wyn Evans,¹ Takafumi Tsukui,³ Hillary Davis,² Joss Bland-Hawthorn,² Jason L. Sanders,⁴ Oscar Agertz⁵

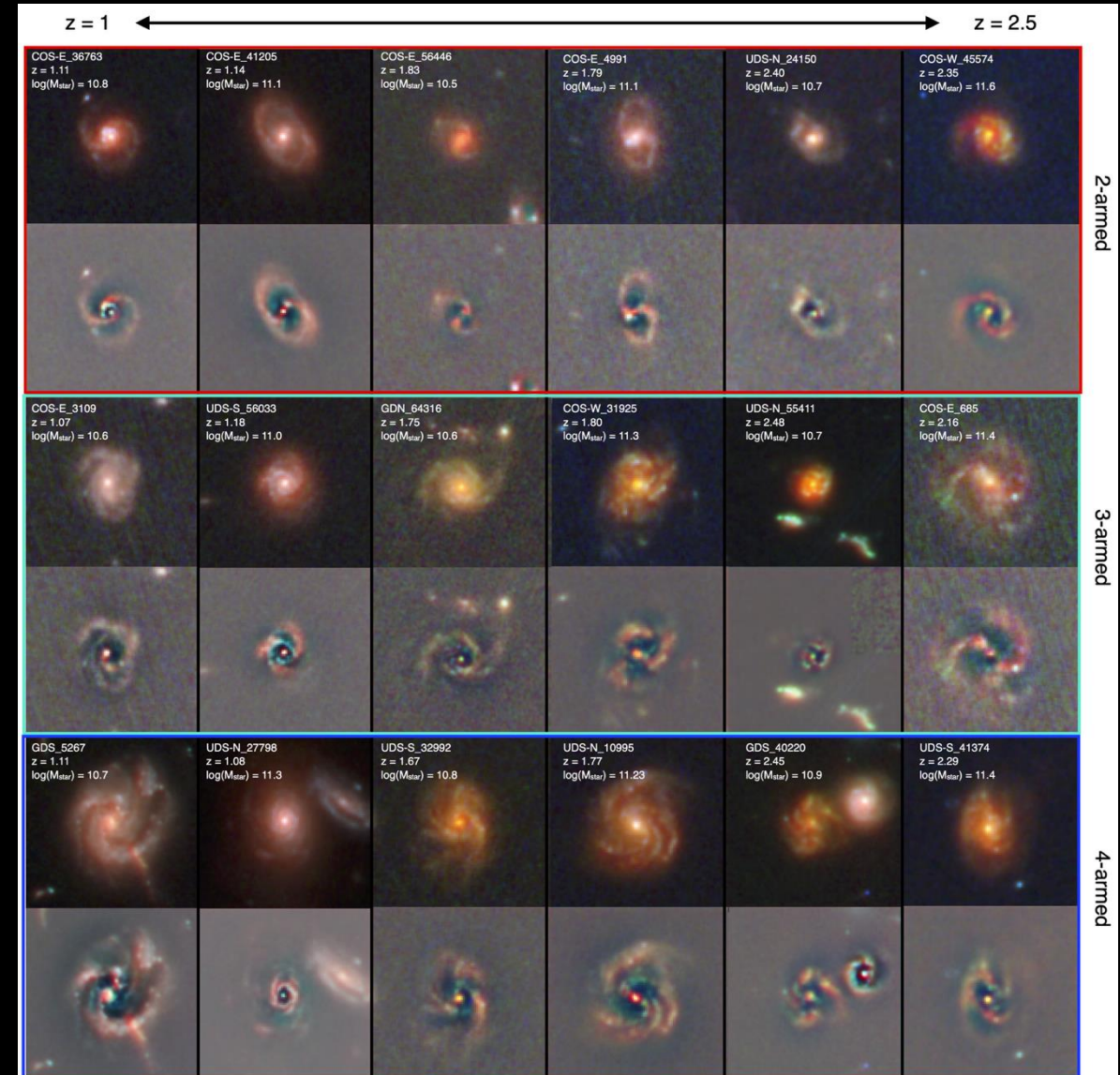




Galaxies at high- z

- Disc substructures (like bar and spiral) already appeared at the early time of the Universe

van der Wal & Meidt 2025



See also Ferreira+23, Kuhn+24, Espejo Salcedo+25 etc.

Galaxies at high- z

- Disc substructures (like bar and spiral) already appeared at the early time of the Universe
- Tracing morphological evolution of galaxies through cosmic time

thin and thick disk galaxies



thick disk only galaxies



Galaxies at high- z

@ESA/Gaia/DPAC

- Disc substructures (like bar and spiral) already appeared at the early time of the Universe
- Tracing morphological evolution of galaxies through cosmic time
- Link Milky Way to the morphological evolution of high- z galaxies
- What is the evolutionary pathway of the Milky Way's disc

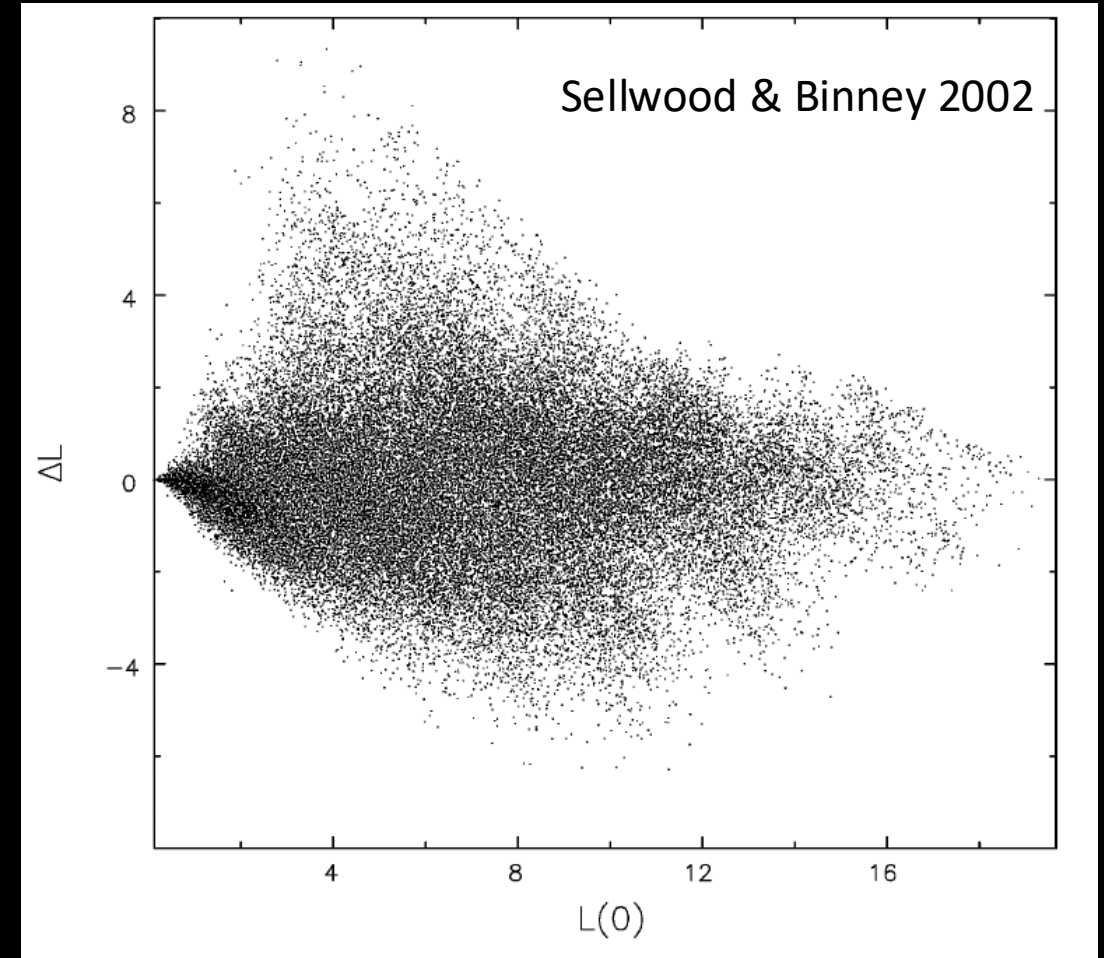




How do stars move after
they formed?

Secular evolution in the Galactic disc

- Orbits of stars do not remain constant
- Stars could move from their birth radius to their present-day radius, called radial migration
- This process happens through interaction with non-axisymmetric perturbations, e.g. the transient spiral arms, galactic bar.

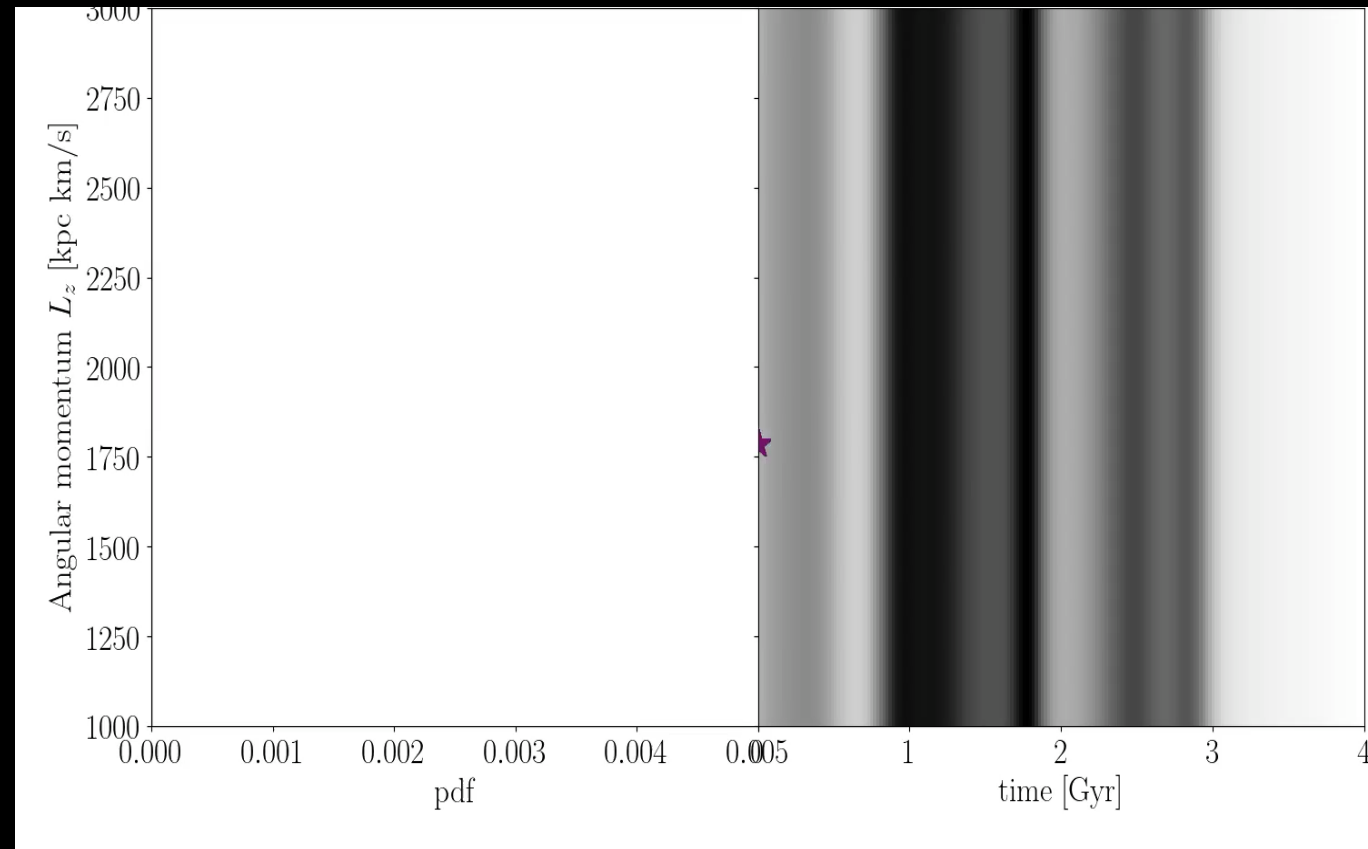


See Sellwood & Binney 02, Minchev & Famaey 10, Halle+15, Khoperskov+20, Haywood+24, Marques+25 (etc...) for different radial migration mechanisms

Secular evolution in the Galactic disc

Credit: Neige Frankel

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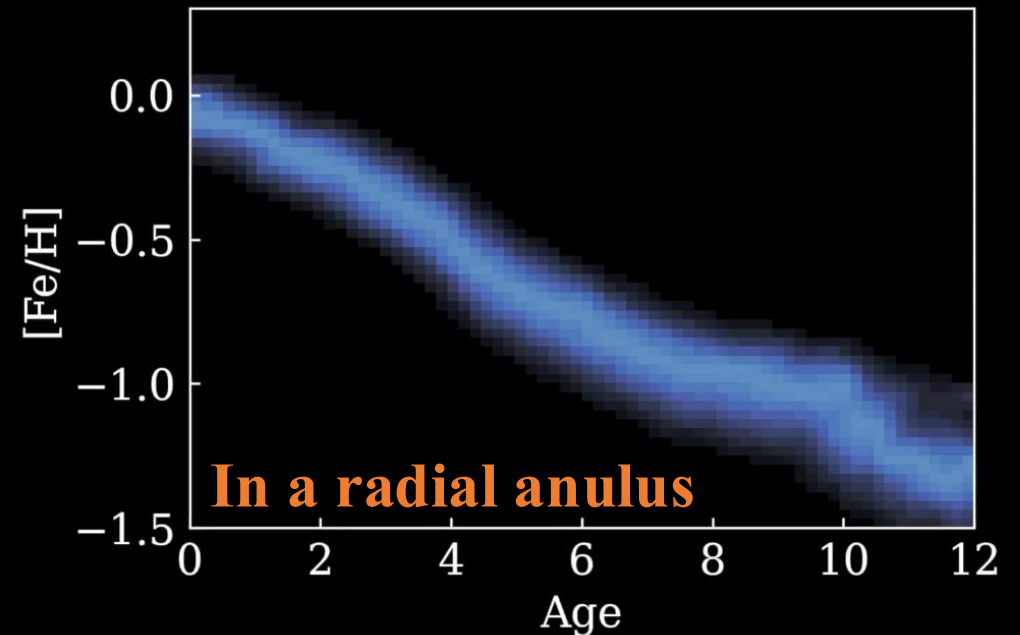
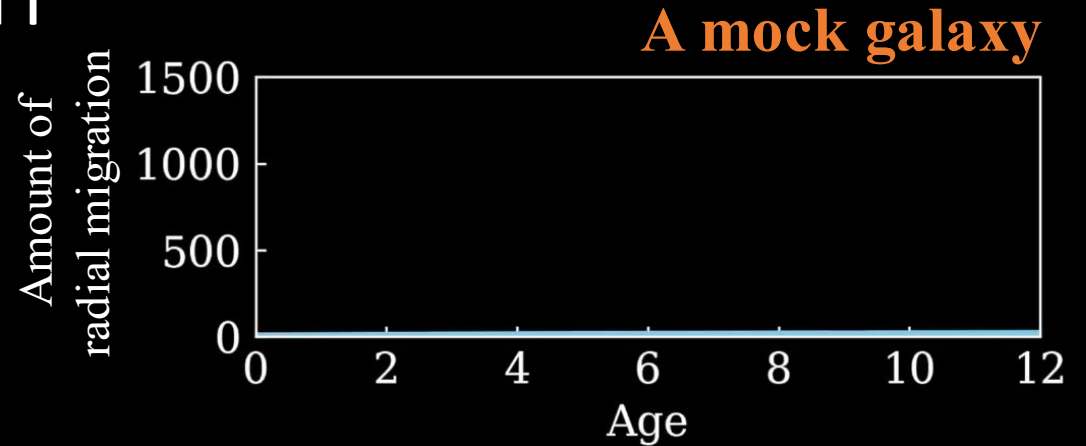


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Signatures of radial migration

- As the Galactic ISM are axisymmetric within $\lesssim 0.1$ dex (Wenger+19, etc.), the observed stellar metallicity in the solar neighbourhood should have little spread at each ages.
- The large metallicity spread in the stellar metallicity at each age reflects the amount of radial migration in the Galactic disc.

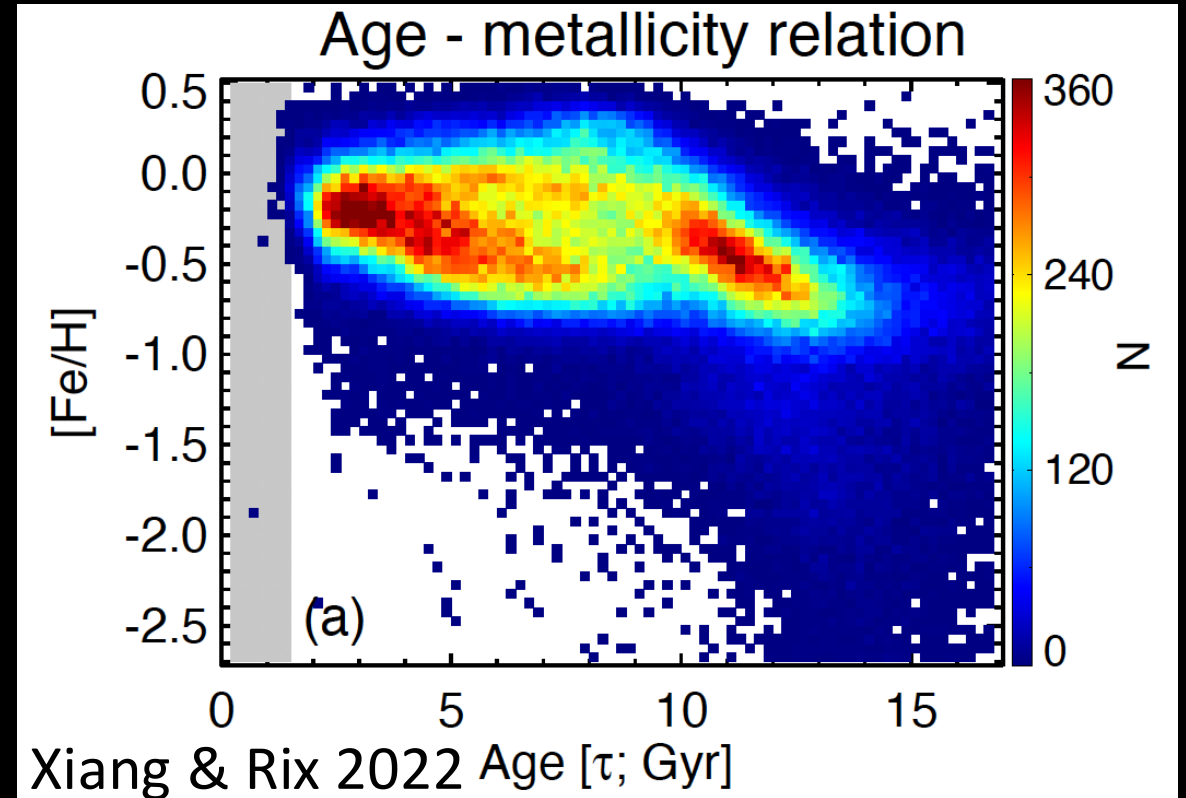
$$\sigma_{L_z} \sim \frac{V_c \sigma_{[\text{Fe}/\text{H}]}}{|d[\text{Fe}/\text{H}]/dR|}$$



Signatures of radial migration

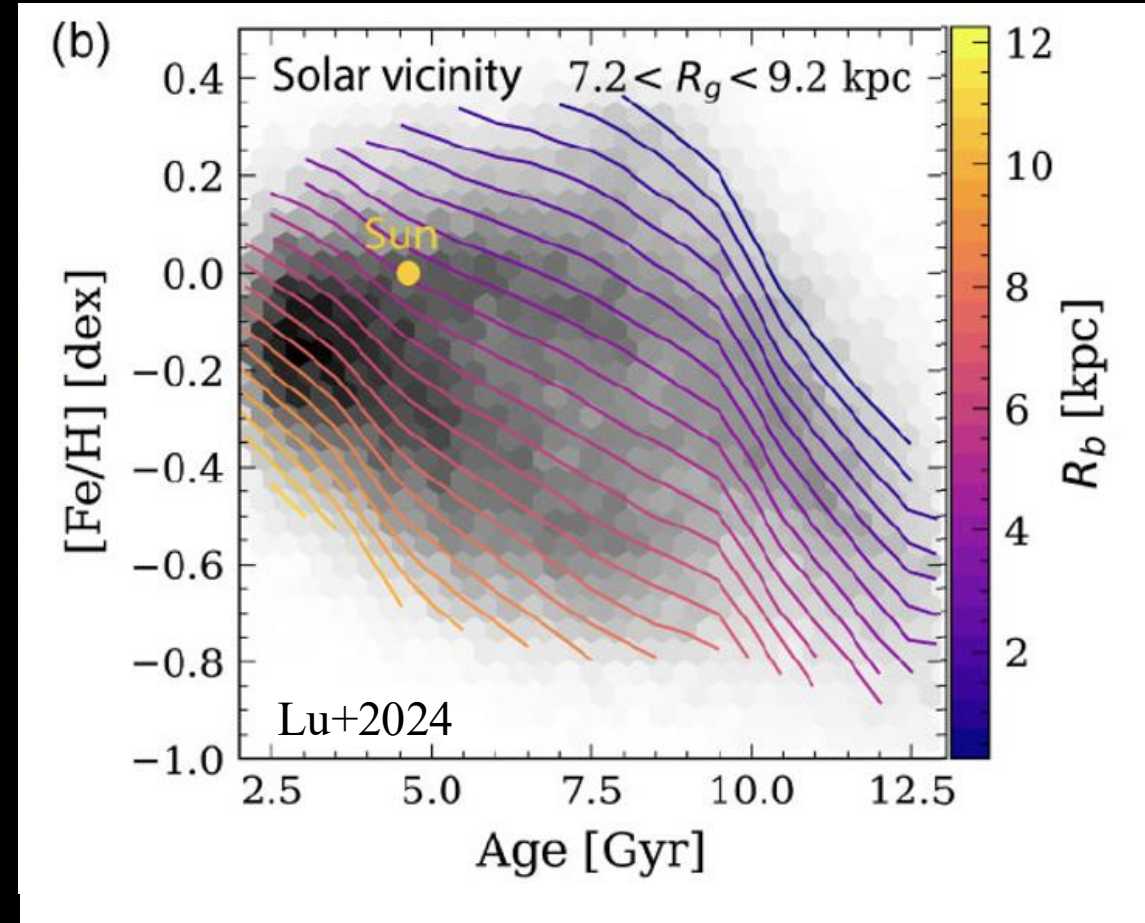
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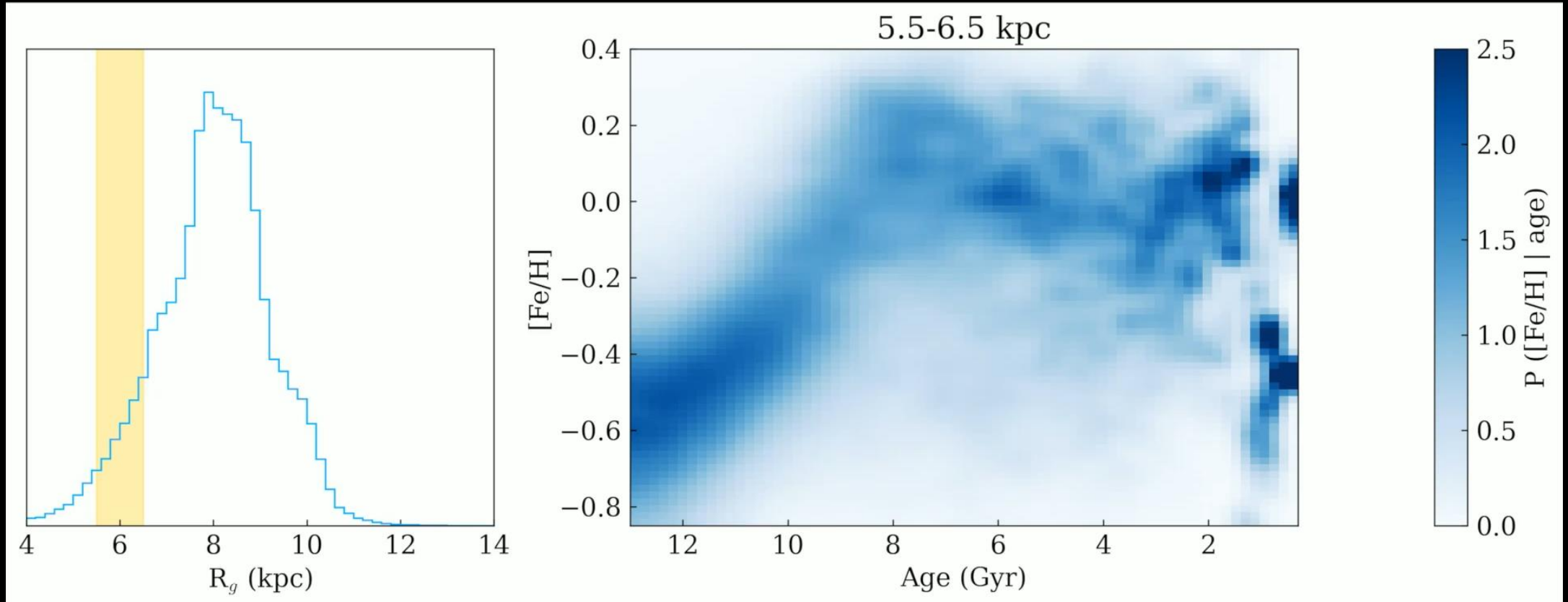


One way of solving this: birth radius inference

- Can estimate birth radii R_b of stars from stellar ages and metallicity:
 $\{\tau, [\text{Fe}/\text{H}]\} \rightarrow R_b$
- ISM metallicity model $[\text{Fe}/\text{H}](R_b, \tau)$
 $[\text{Fe}/\text{H}](R_b, \tau) = [\text{Fe}/\text{H}]_0(\tau) + \nabla[\text{Fe}/\text{H}]R_b$
 - 1) maximum metallicity at each age
 - 2) metallicity spread at each age
- One can then comparing R_{today} and R_b to map the secular evolution



LAMOST: Age vs $[\text{Fe}/\text{H}]$ vs R_g



Test-particle simulation: bar-driven migration

Initialise a quasi-isothermal disc in an axisymmetric disc potential

Grow a galactic bar in the background potential with an initial pattern speed
 $\Omega_i = 80 \text{ km/s/kpc}$
($R_{CR,init} \sim 3 \text{ kpc}$)

Bar reach its maximum strength and start decelerate with
 $\eta = -\dot{\Omega}/\Omega^2 = 0.003$

Final pattern speed
 $\Omega_0 = 34 \text{ km/s/kpc}$
($R_{CR,0} \sim 7 \text{ kpc}$)



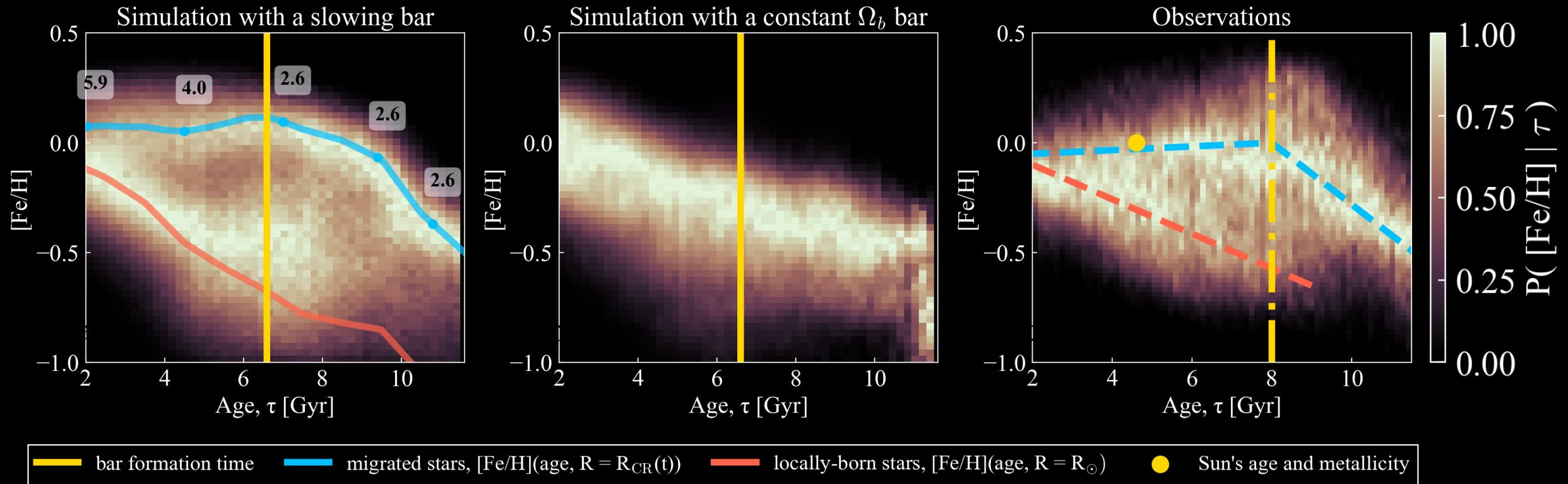
Add new disc stellar particles into the simulation constantly with time

Assign metallicity to the test particles afterwards with a model
 $[\text{Fe}/\text{H}] = f(R_b, \tau)$

Cut $d_{sun} < 3 \text{ kpc}$ to mimic the coverage of the subgiant sample

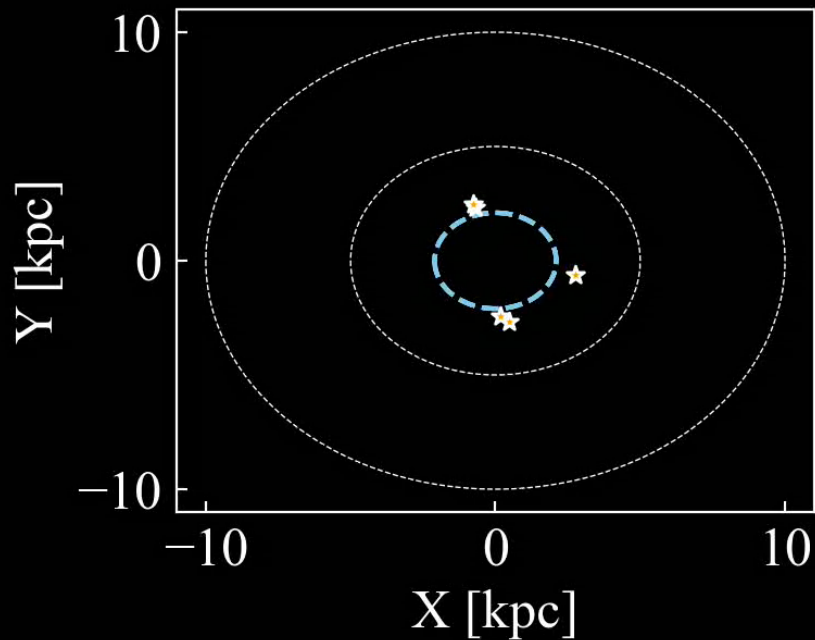
Resulting age-metallicity sequences

Local stars vs. migrated stars

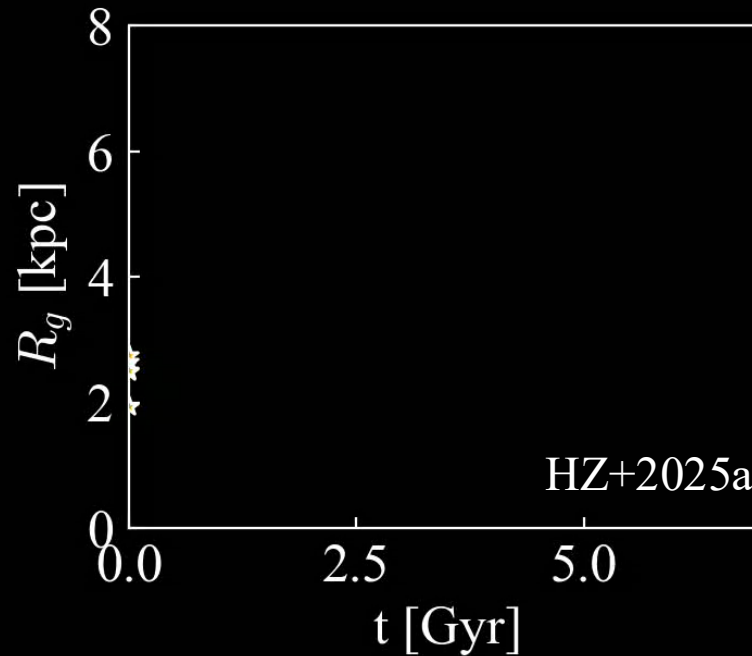


Resonant dragging of a decelerating bar

A toy demonstration



$t = 0.00$ Gyr
No bar, axisymmetric disc



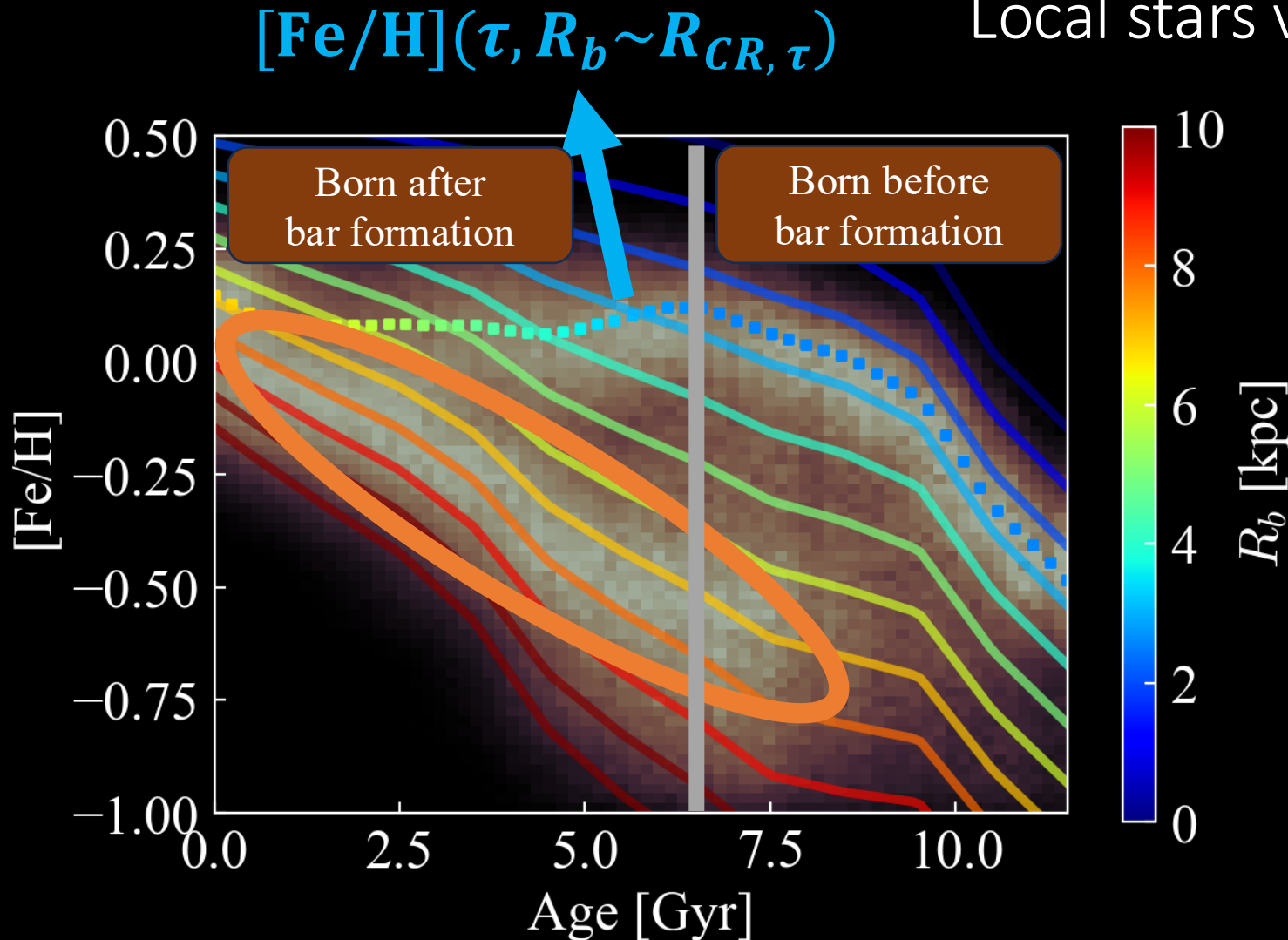
Stars trapped in the corotation resonance migrate with the expansion of the corotation. This brings stars from the inner Milky Way to the present-day corotation radius.

See Chiba+21; Chiba & Schonrich 2021 for analytic descriptions

Today's pattern speed $\sim 32 - 34$ km/s/kpc (Chiba+21, Clarke+22, HZ+24, Dillamore+25); corotation radius $\sim 7 - 7.5$ kpc

Resulting age-metallicity sequences

Local stars vs. migrated stars



Stars born **before bar formation**:
those that has $R_b \sim R_{CR, init}$
experience strong resonance
dragging



Age-metallicity sequence
tracks $[\text{Fe}/\text{H}](\tau, R_b \sim R_{CR, init})$

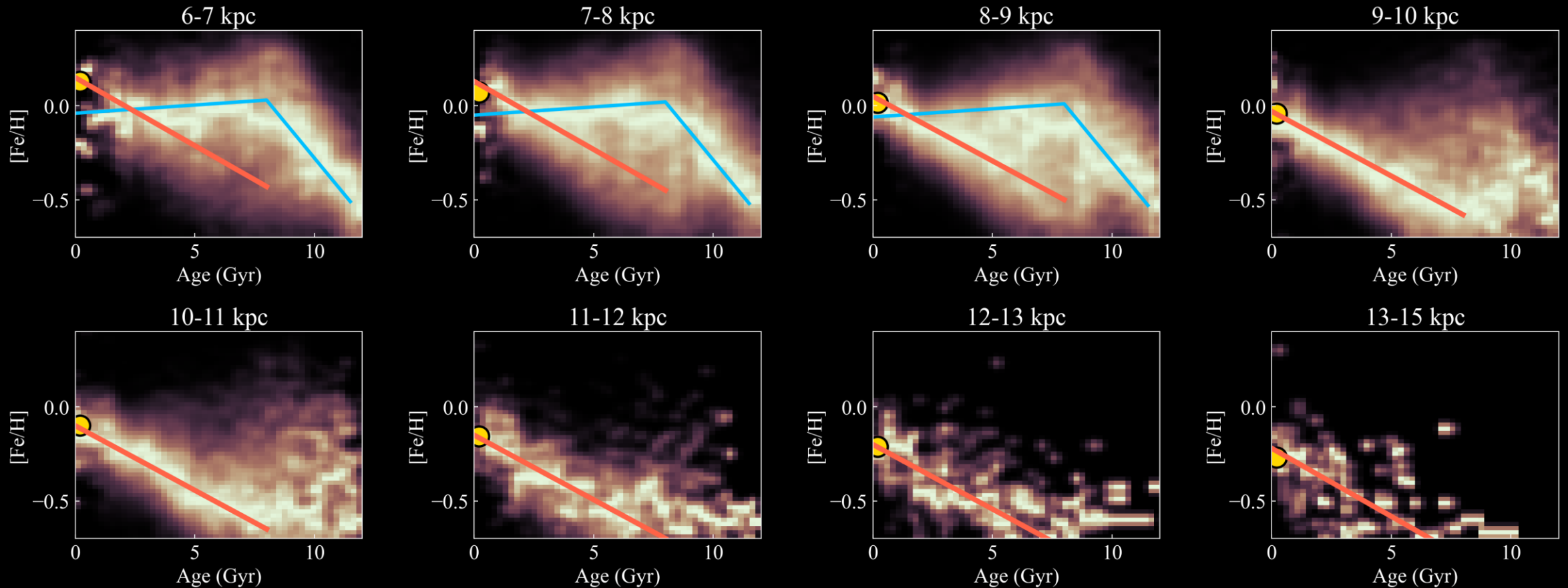
Stars born **after bar formation**:
those that has $R_b \sim R_{CR}(t = \tau)$
experience strong resonance
dragging



Age-metallicity sequence flattens,
and tracks $[\text{Fe}/\text{H}](\tau, R_b \sim R_{CR, \tau})$

Resulting age-metallicity sequences

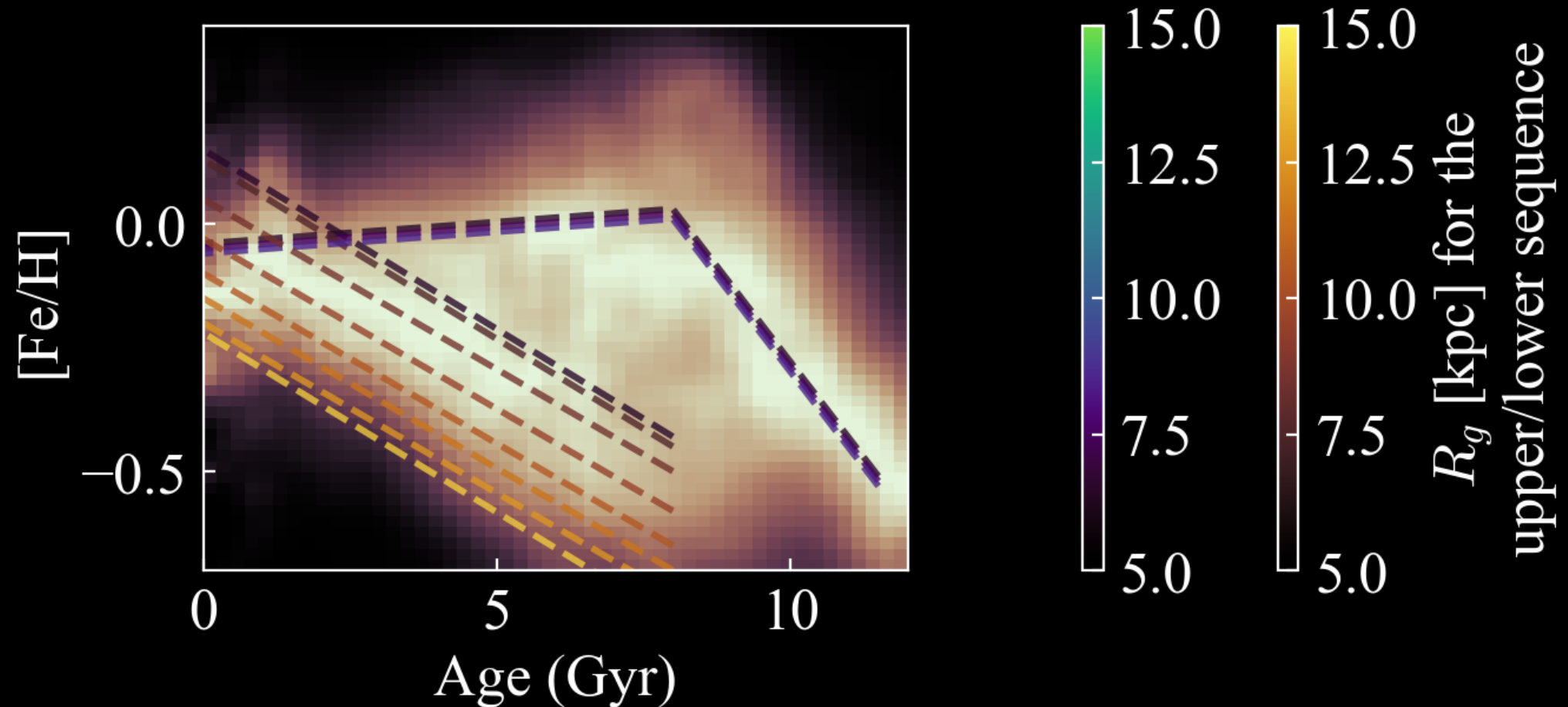
The guiding radii dependence



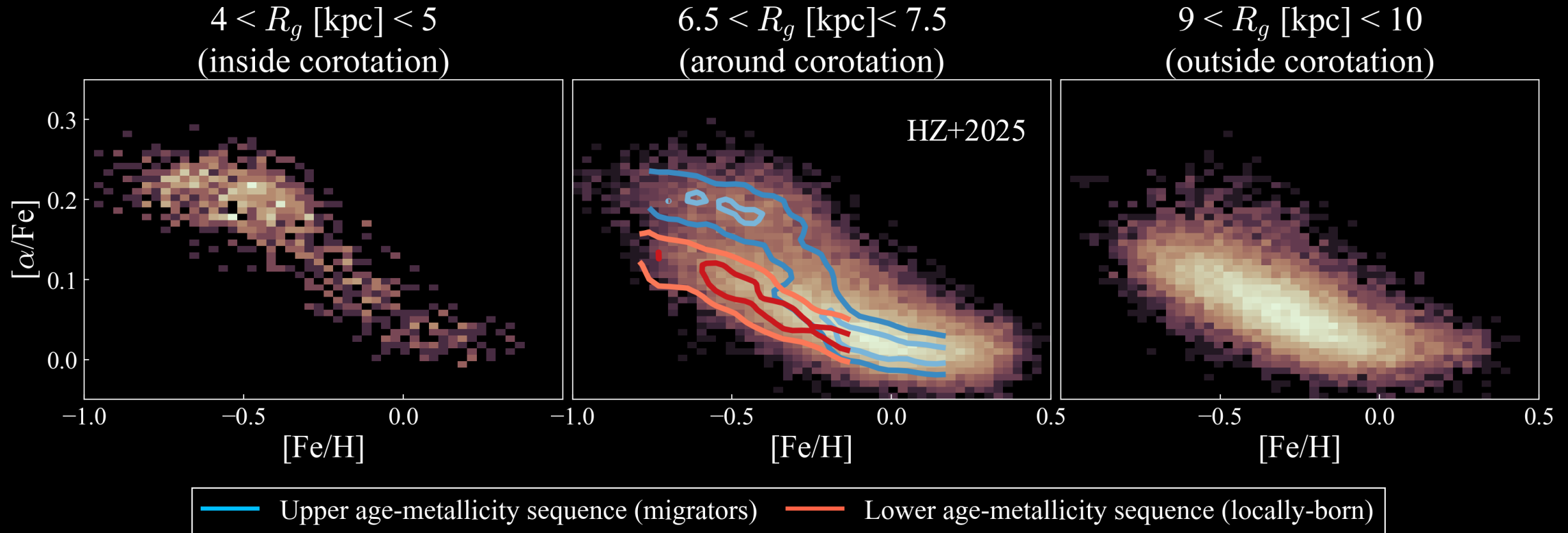
● = gas-phase metallicity today

Resulting age-metallicity sequences

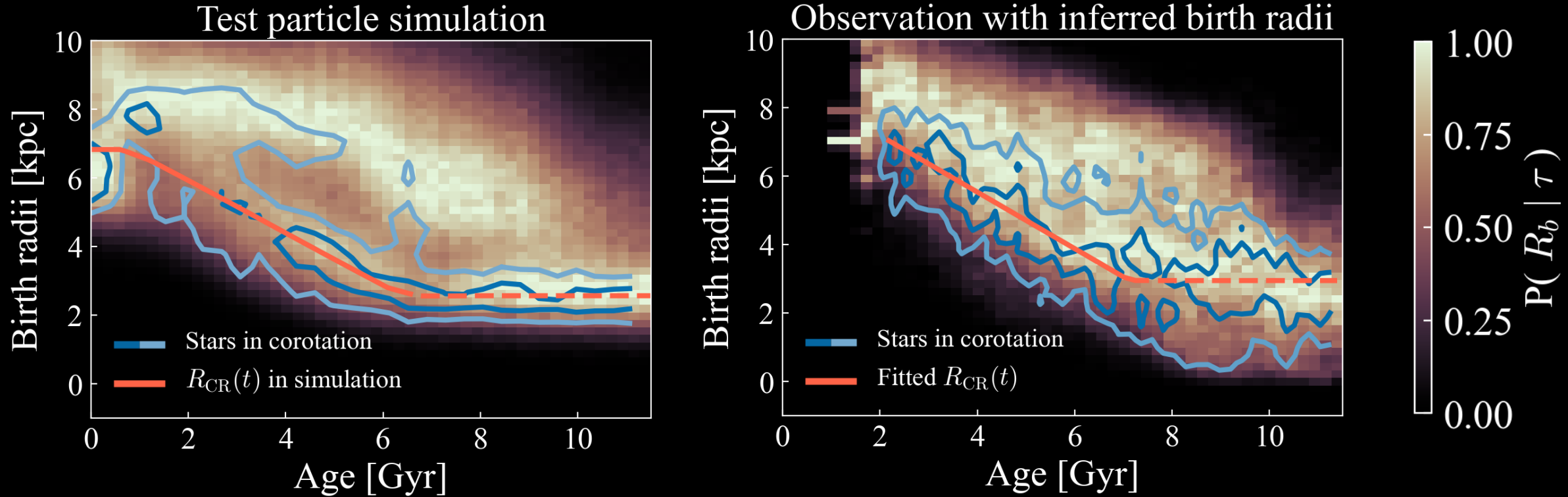
The guiding radii dependence



Implications: $[\alpha/\text{Fe}] - [\text{Fe}/\text{H}]$ bimodality



Inferring the pattern speed history of the bar



In this birth radius calculation method (Lu+24), we can infer:

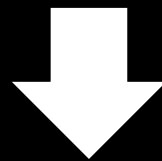
$$t_{bf} \sim 6 - 8 \text{ Gyr}; \Omega_i \sim 60 - 80 \text{ km/s/kpc}; \eta = -\dot{\Omega}/\Omega^2 \sim 0.0025 - 0.004$$

agree with other independent measurements of t_{bf} and η (Chiba+21, Sanders+24), and non-independently Haywood+24

Half-time break

- Corotation resonance of decelerating bar can create the V-shaped age-metallicity pattern
- Can be used to explain the α -bimodality of the disc
- Can infer the history of bar deceleration (e.g. formation time, initial pattern speed and deceleration rate) using this signature.

Next: A more comprehensive chemodynamical forward modelling approach



Chemo-chrono-dynamical modelling

- Fitting for the column-normalised age-metallicity plane at different radial bins

$$p([Fe/H]|\tau, R_g) = \frac{p([Fe/H], R_g|\tau)}{\int d[Fe/H] p([Fe/H], R_g|\tau)}$$

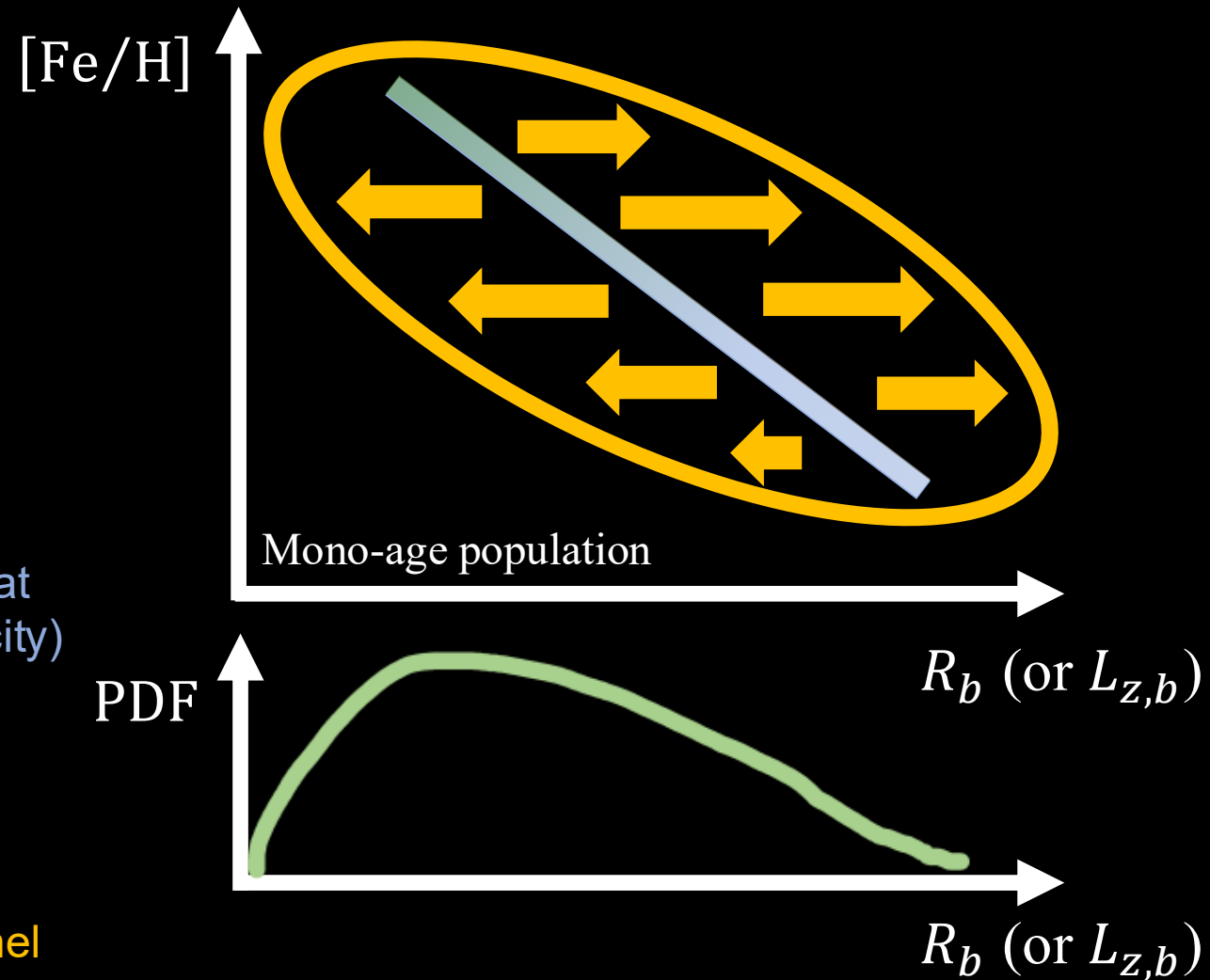
where $p([Fe/H], R_g|\tau) =$ Stellar metallicity at birth (ISM metallicity)

$$\int dL_{z,b} \{ p([Fe/H]|\tau, L_{z,b})$$

$$p(L_{z,b}|\tau) p(L_z|\tau, L_{z,b}) \}$$

Initial radial profile

Radial migration kernel



Chemo-chrono-dynamical modelling

With observables: $\{\tau, [\text{Fe}/\text{H}], x, y, z, v_x, v_y, v_z\}$

Disc growth

$$p(L_{z,b}|\tau) \propto L_{z,b} \exp\left[-\frac{L_{z,b}}{V_{\text{circ}} R_{d,0}}\right]$$

$$R_{d,0}(\tau)$$

Initial disc scale length
(Star-forming disc
scale length)

Weak chemical tagging

$$[\text{Fe}/\text{H}]_{\text{ISM}} = [\text{Fe}/\text{H}]_0 + \nabla[\text{Fe}/\text{H}] R_b$$

$$\nabla[\text{Fe}/\text{H}](\tau)_{\text{(ISM)}}$$

Radial metallicity
gradient at birth
(Gas-phase
metallicity gradient)

Orbital diffusion

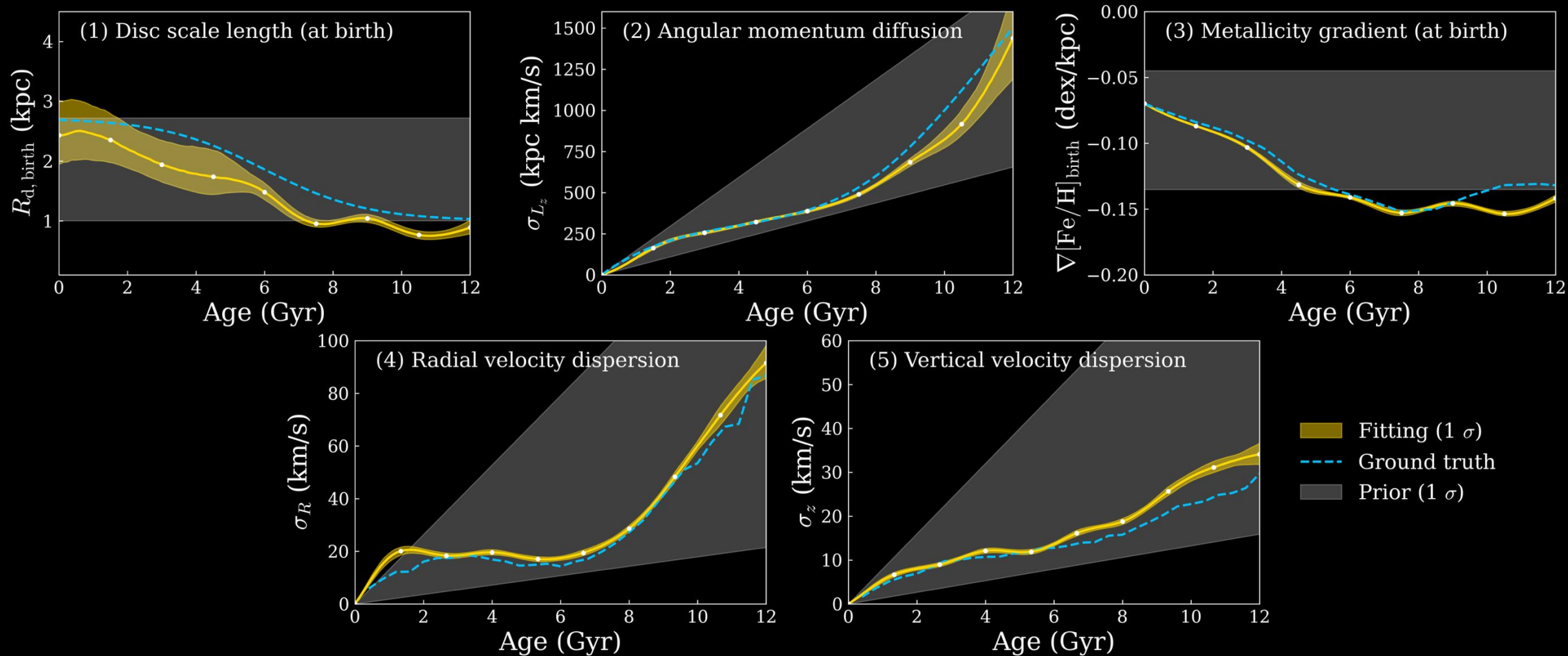
$$p(L_z|L_{z,0}, \tau) = \mathcal{N}\left(L_z \left| L_{z,b} - \frac{\sigma_{L_z}^2}{2V_{\text{circ}} R_{d,0}}, \sigma_{L_z} \right.\right)$$

$$p(v_R, v_z|R, R_g, z) \propto \exp\left[-\frac{J_R \kappa}{\sigma_R^2}\right] \exp\left[-\frac{J_z \nu}{\sigma_z^2}\right]$$

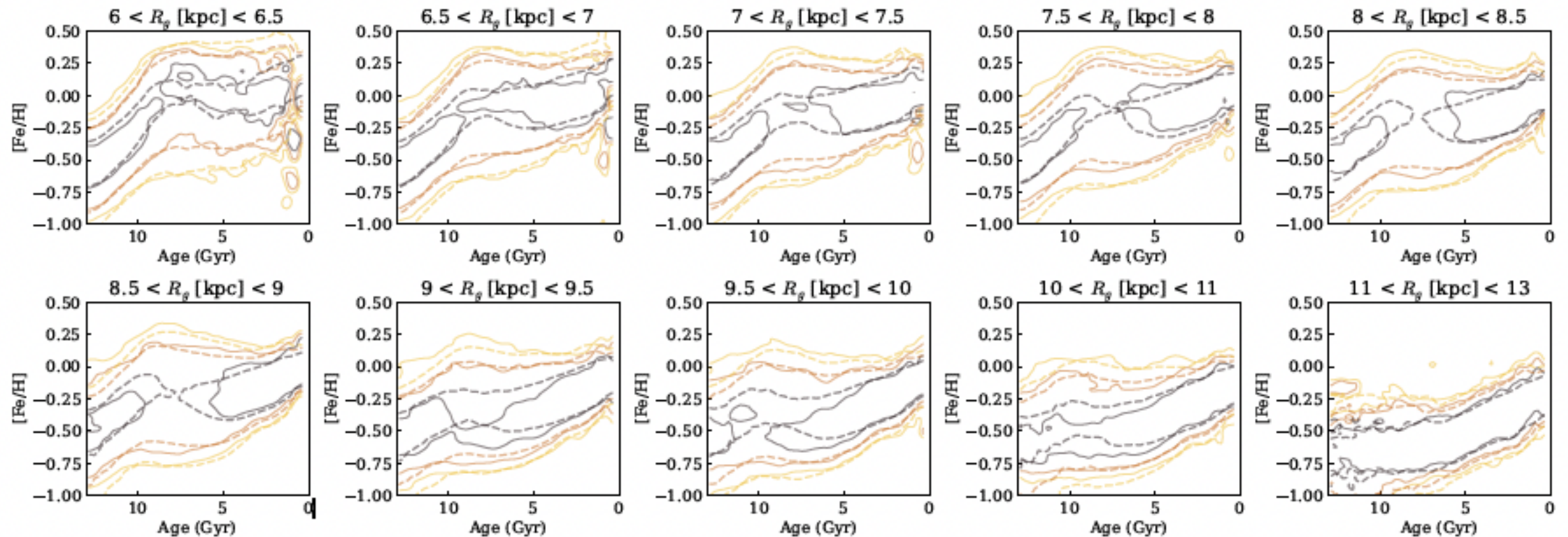
$$\begin{aligned} \sigma_{L_z}(\tau, R_g) \\ \sigma_R(\tau, R_g) \\ \sigma_z(\tau, R_g) \end{aligned}$$

Angular momentum
diffusion coefficient
+
Radial and vertical
velocity dispersion

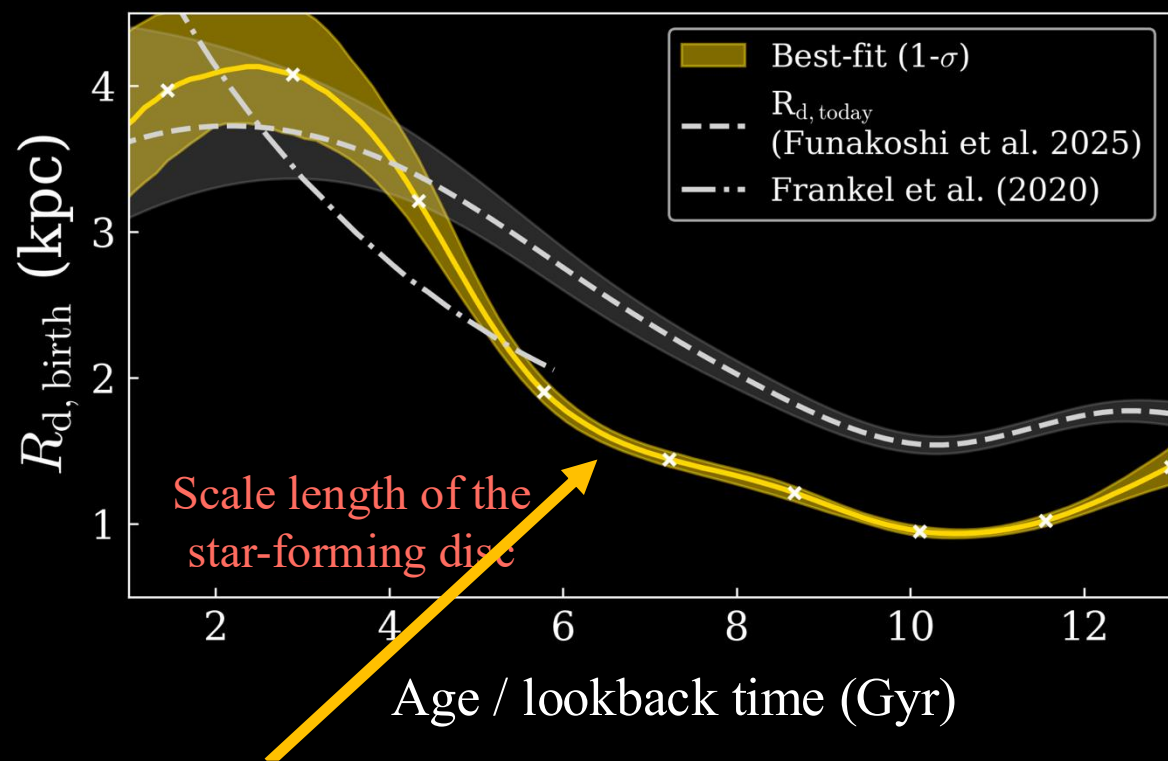
Validation against selection function & uncertainties



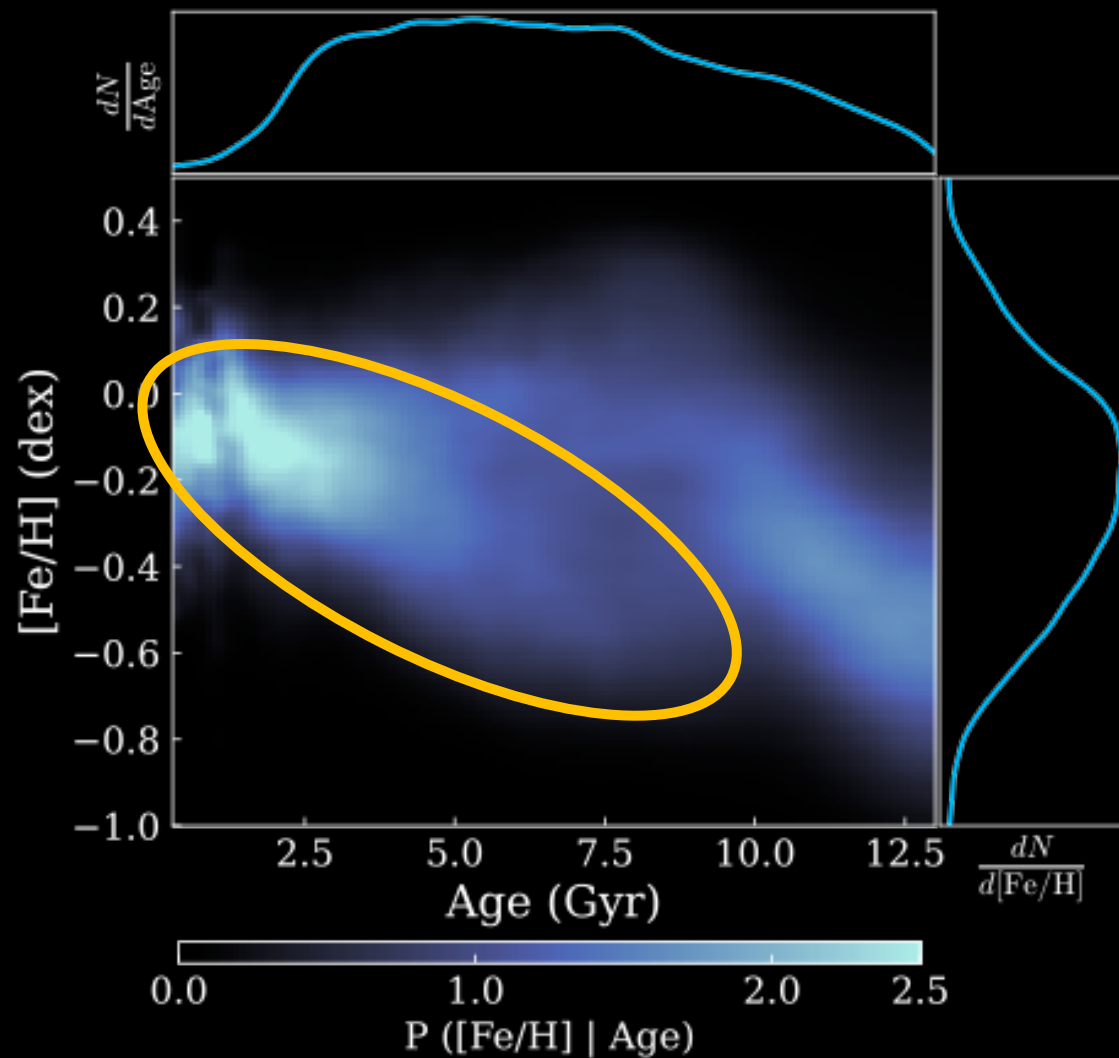
Model fits to data well



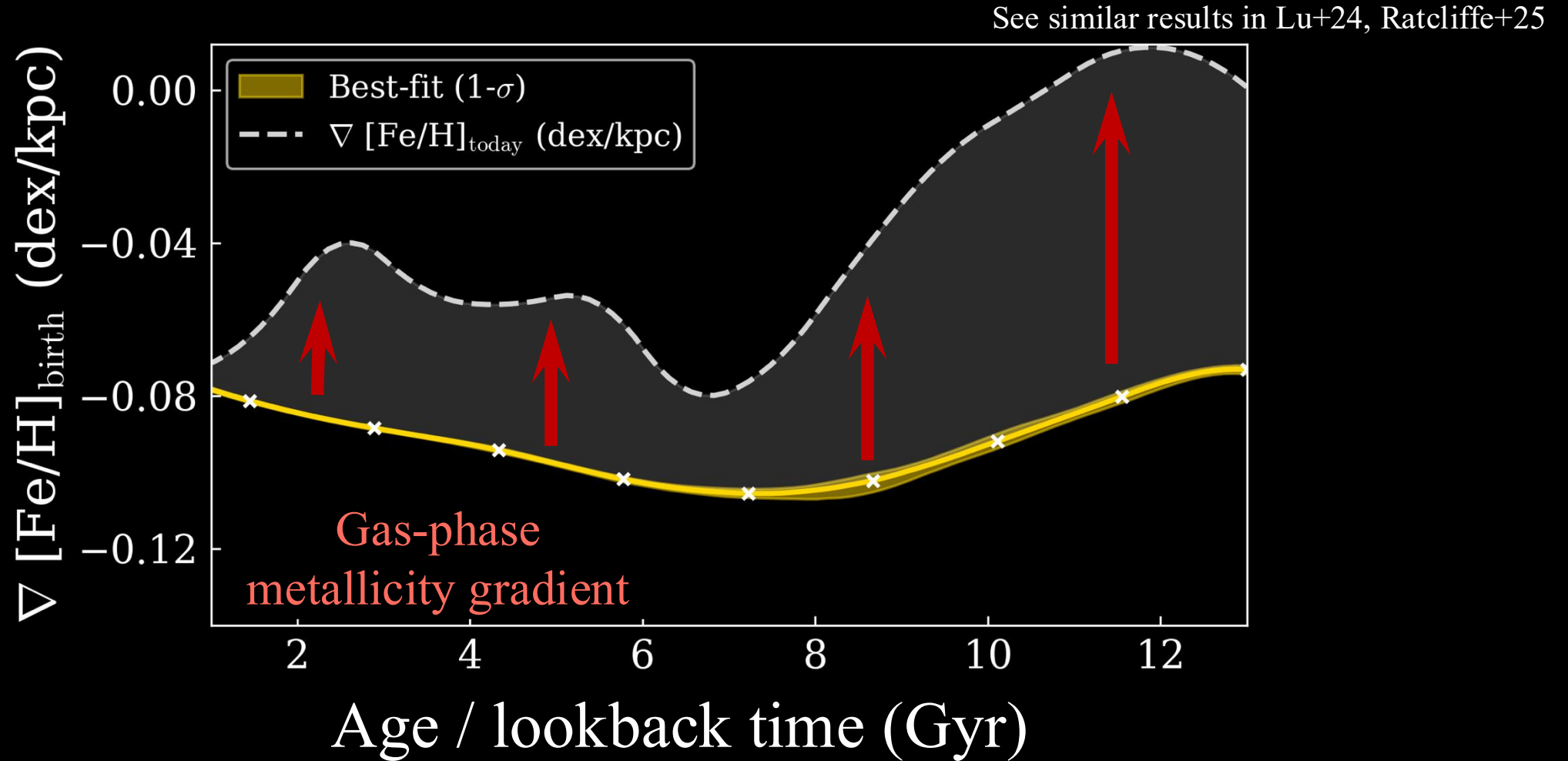
Results: Inside-out formation



Sharp increase in the star-forming disc
scale length: Gas accretion?

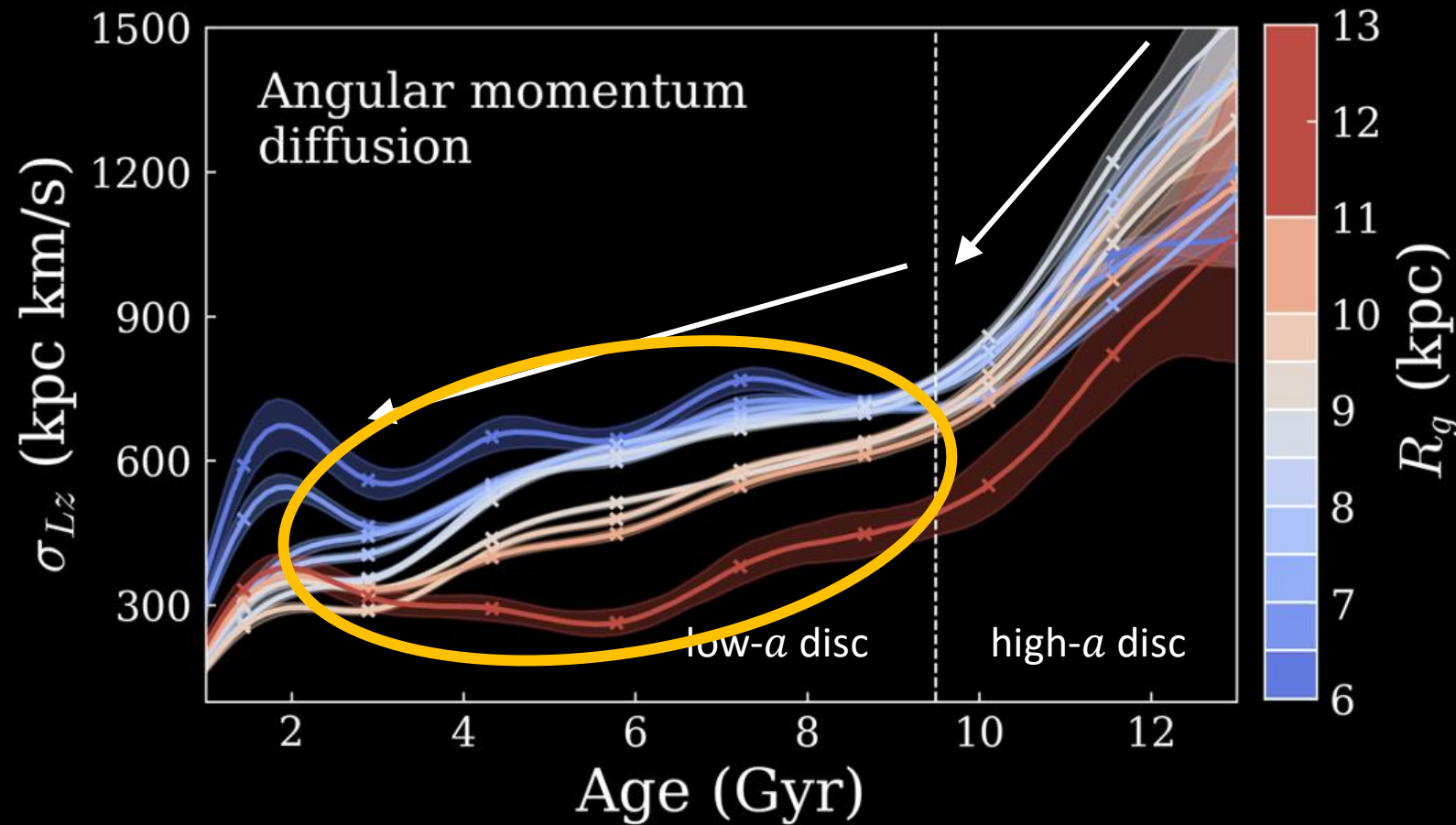


Results: metallicity gradient

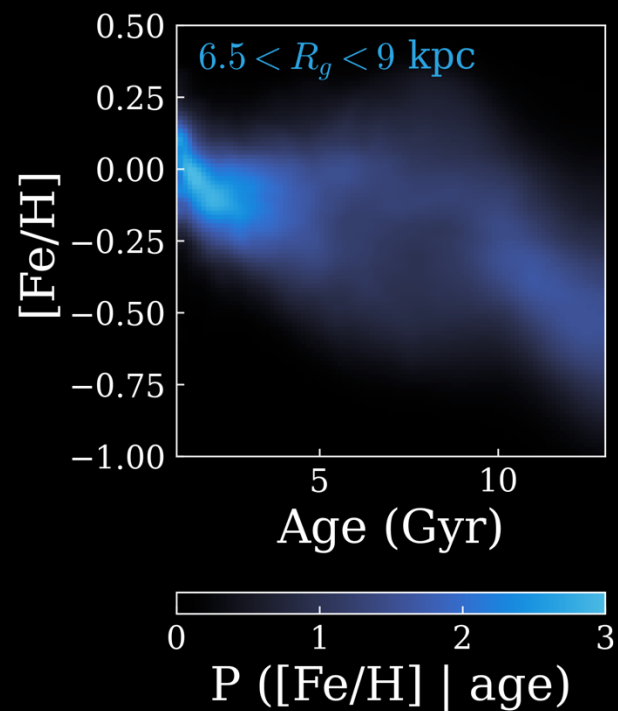
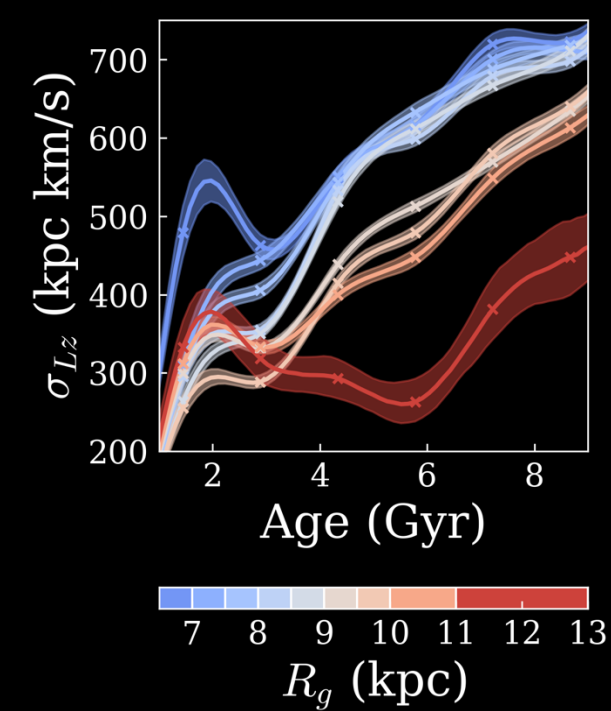


An approximately flat but constantly negative birth metallicity gradient since the disc formation

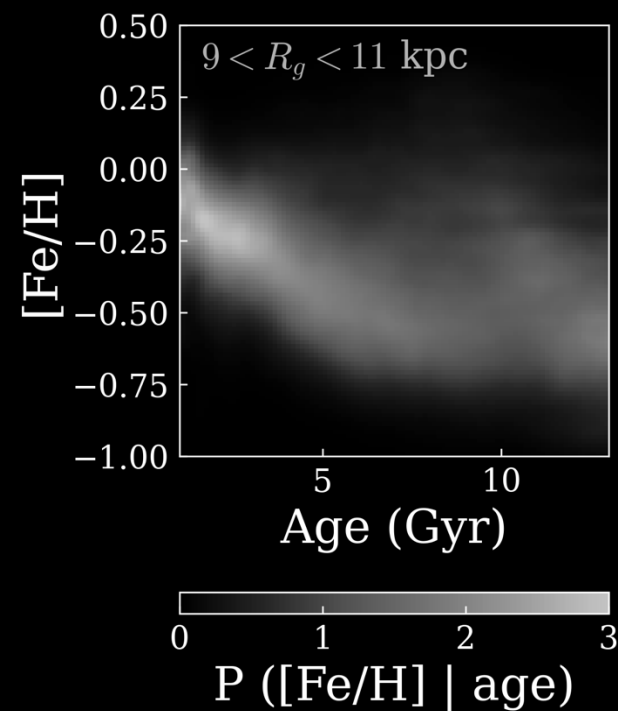
Radial migration strength



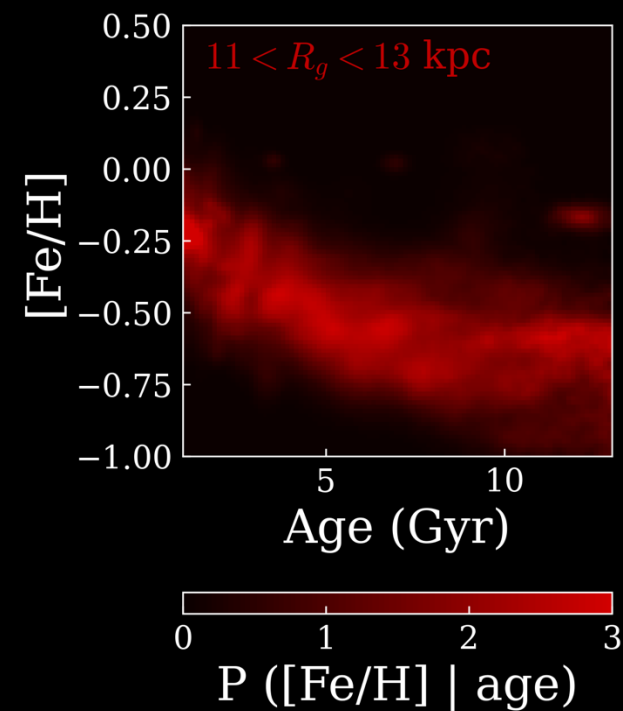
- High angular momentum diffusion in the old, high- a disc compared to the young, low- a disc
- σ_{Lz} is separated into three radial bins
 - 1) $6.5 < R_g / \text{kpc} < 9$
 - 2) $9 < R_g / \text{kpc} < 11$
 - 3) $R_g > 11 \text{ kpc}$



Around
CR

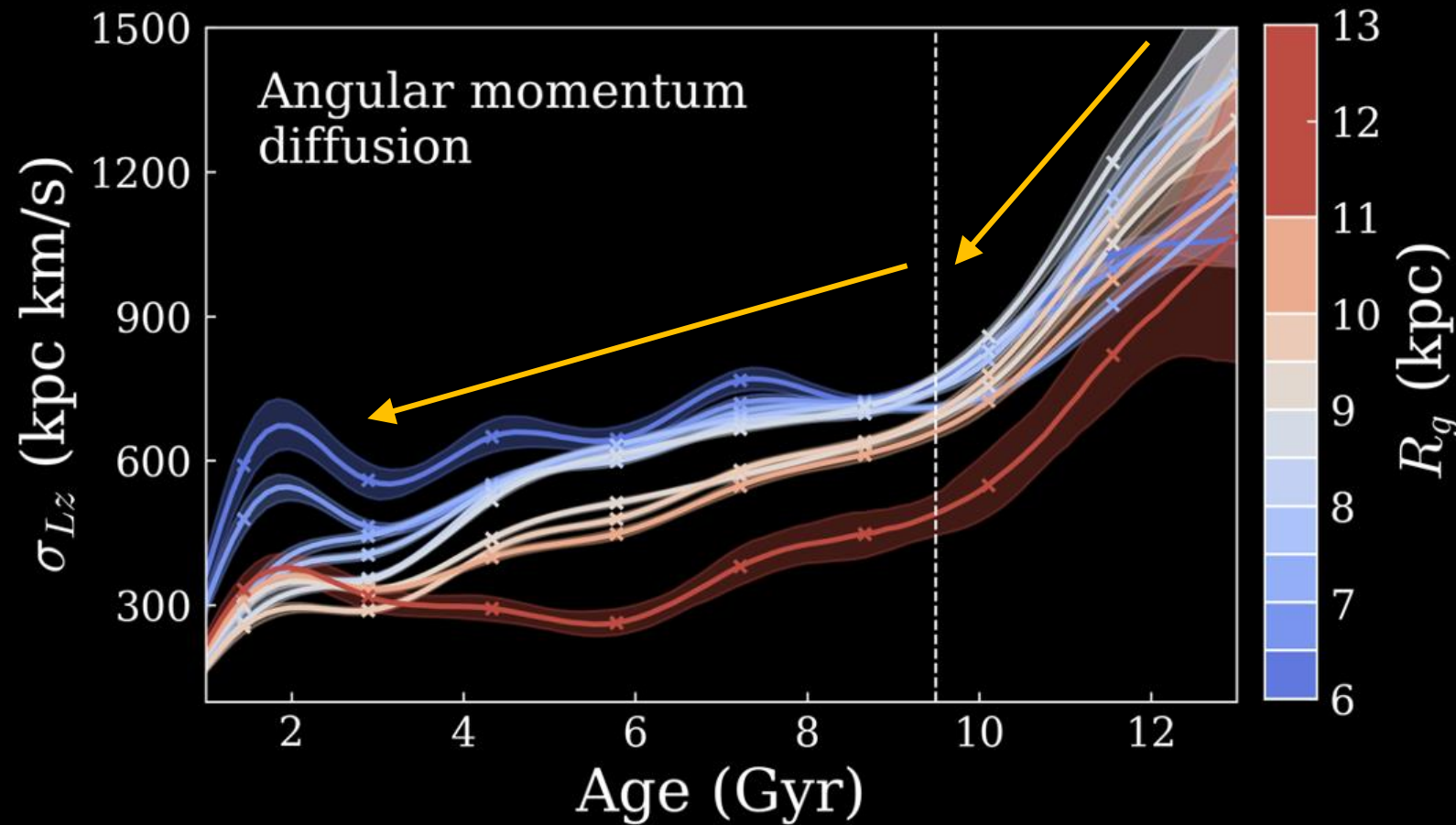


Between
CR & OLR



Outside
OLR

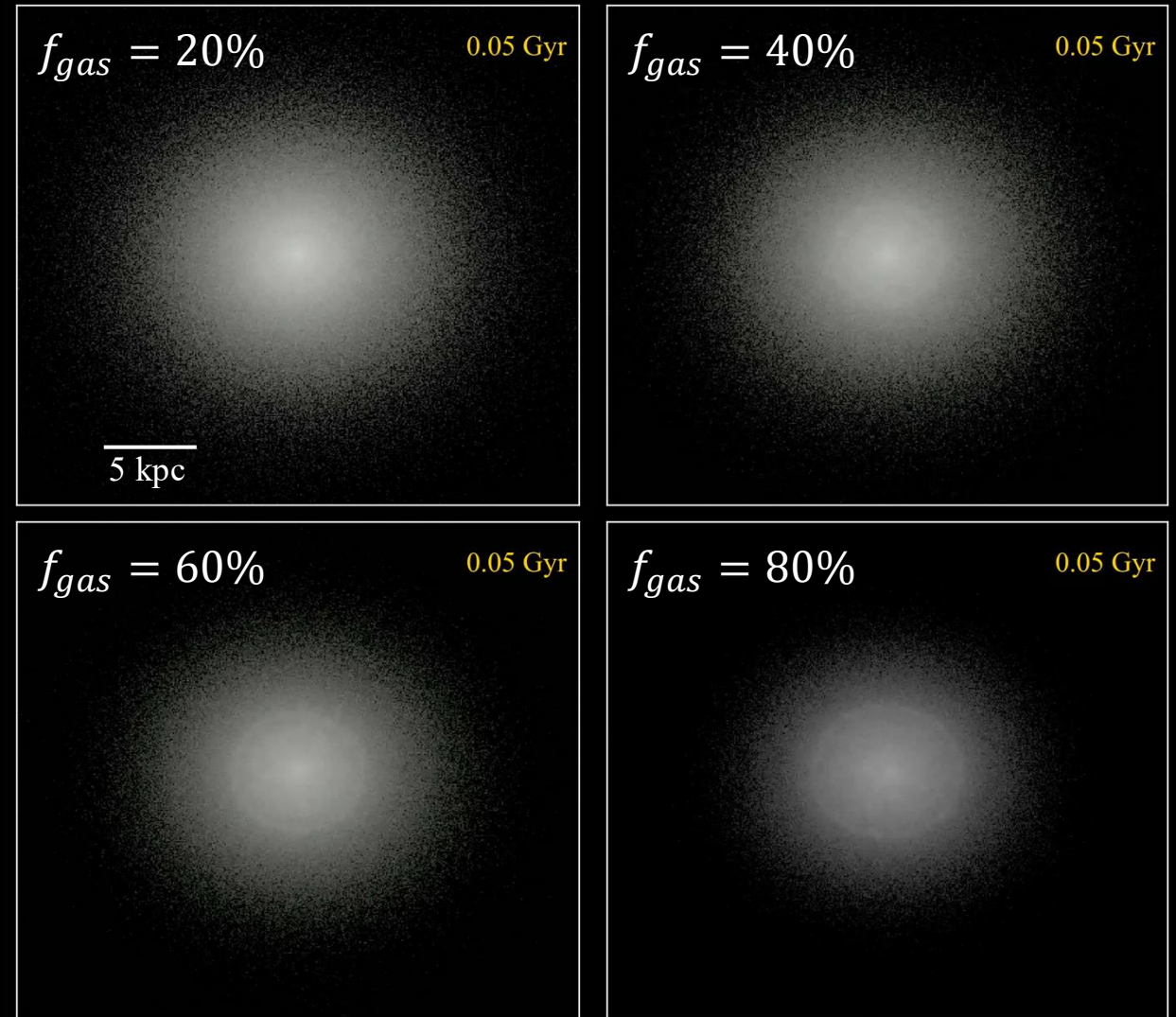
Radial migration strength



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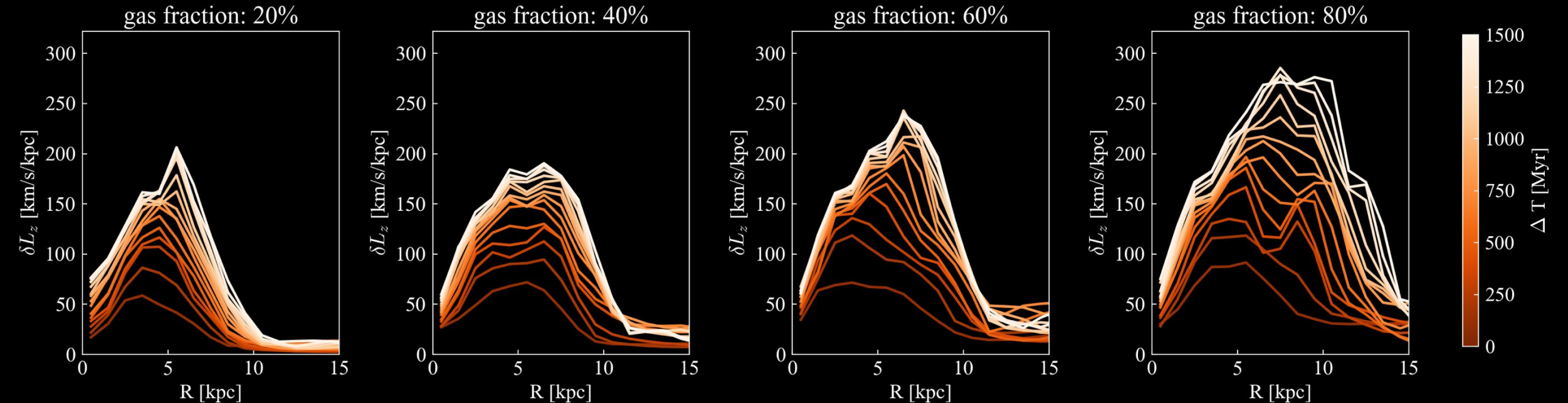
Nexus simulations: the effect of gas

- Same halo and disc mass, but different gas fraction
- Simulation suite:
 - Low-mass MW-analogue ($V_c \sim 140$ km/s) with gas fractions 20/40/60/80%



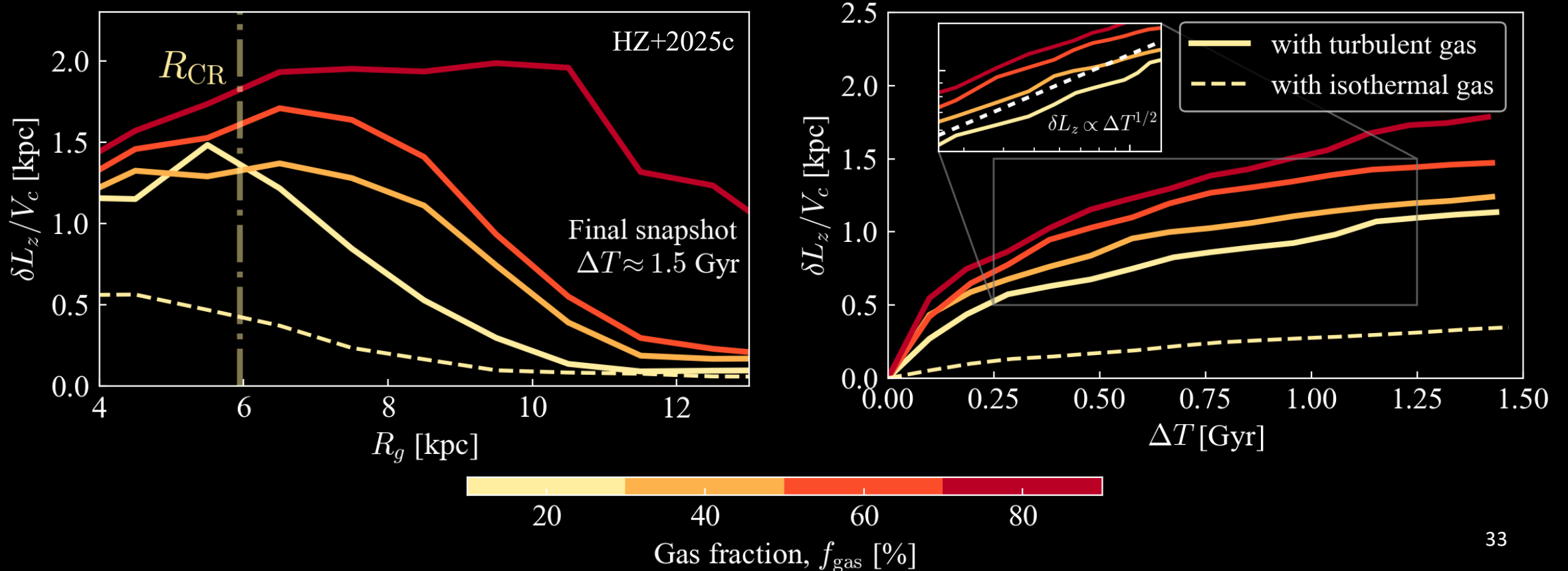
A quick view of the diffusion

- Computing L_z, J_R, J_z of the initial and final state of particles as orbits label
- $\delta X(t) = RMS(\Delta X) = \sqrt{\langle (X(t) - X(0))^2 \rangle}$ for $X = L_z, J_R, J_z$



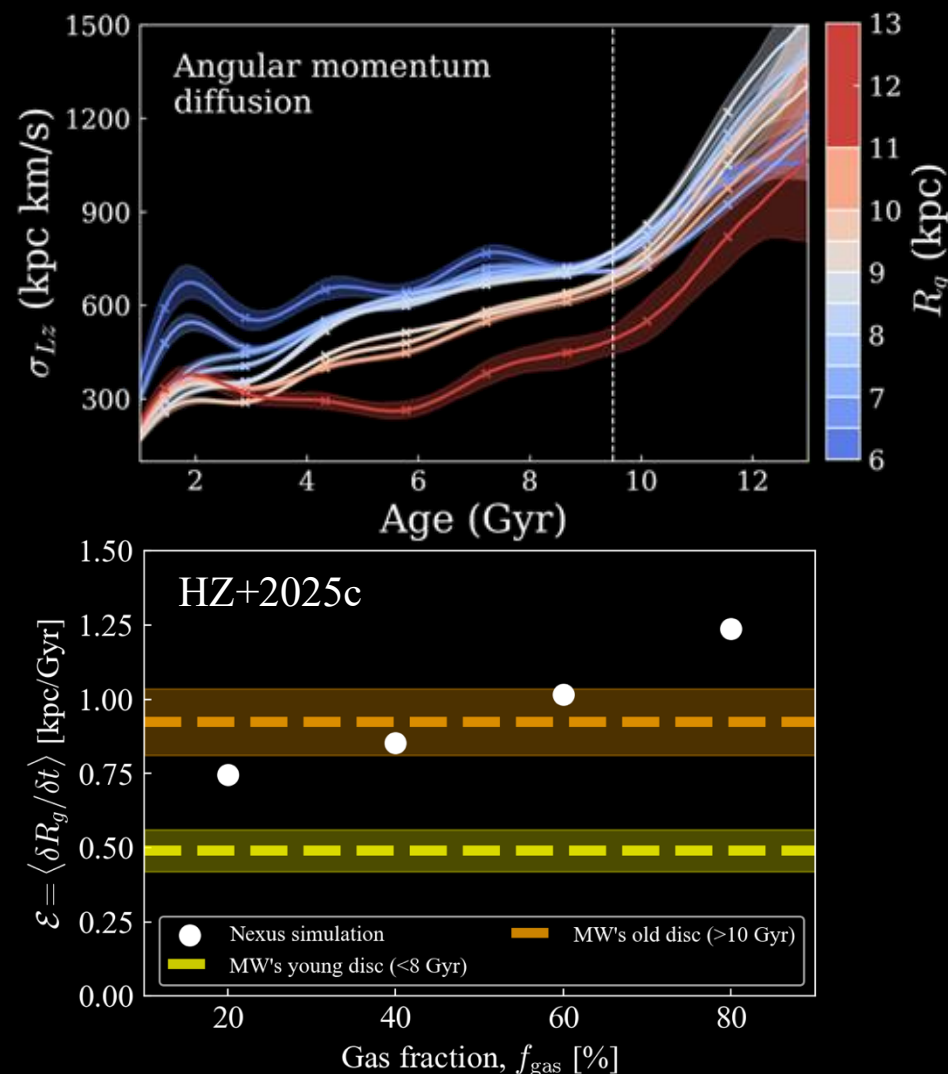
More gas = more diffusion

- More angular momentum diffusion in the more gas-rich disc
- $\delta L_z \propto \sqrt{t}$ in these isolated discs $\rightarrow$ a constant diffusion coefficient



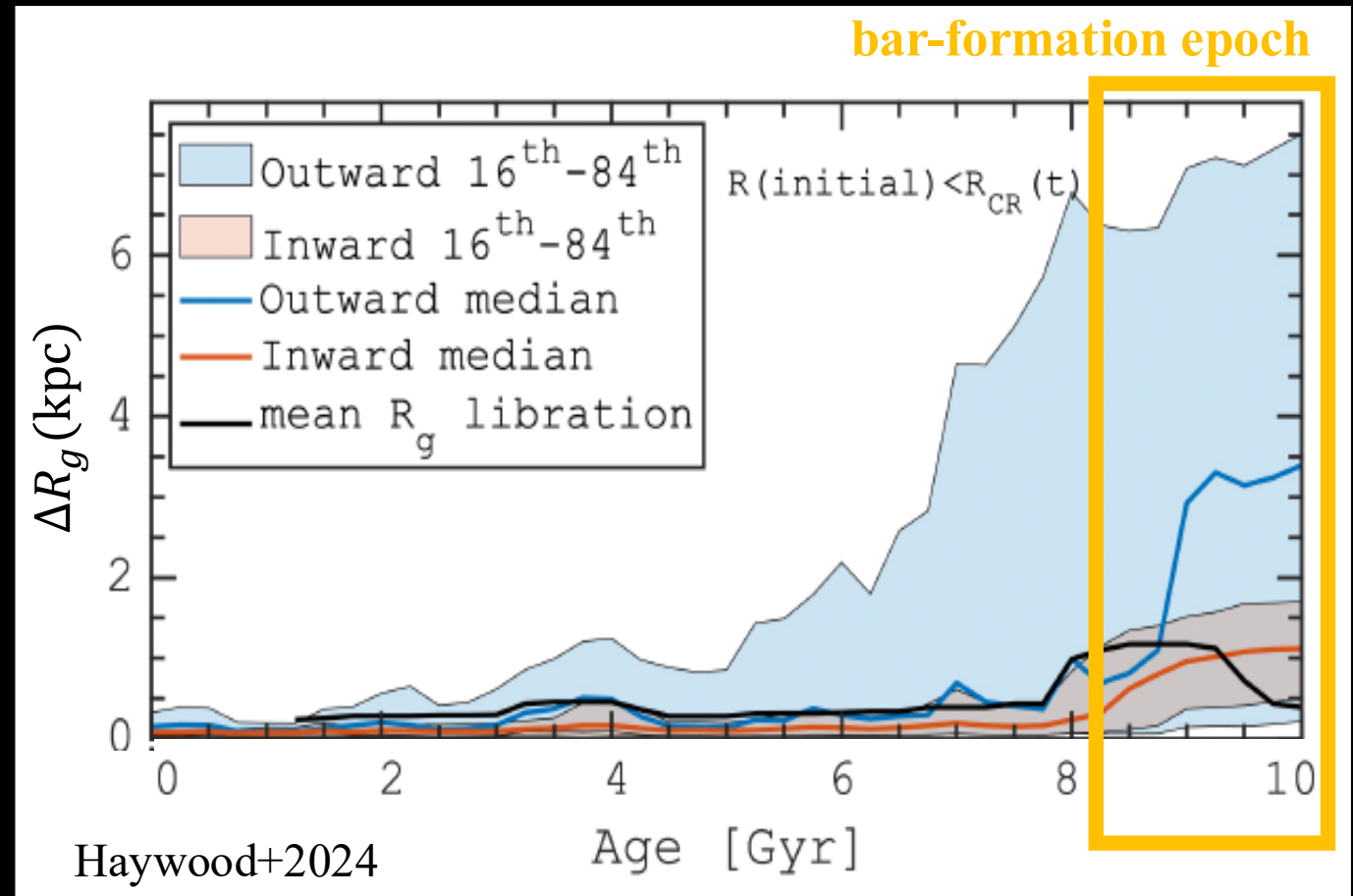
Possible interpretations of the transition in the radial migration strength from high- α to low- α disc

- **Gas-rich to gas-poor disc transition** when the low- α disc formed. (See also the evidence from kinematic fitting in Funakoshi+2025, and also supported by the high-z observation, Tsukui+2025)



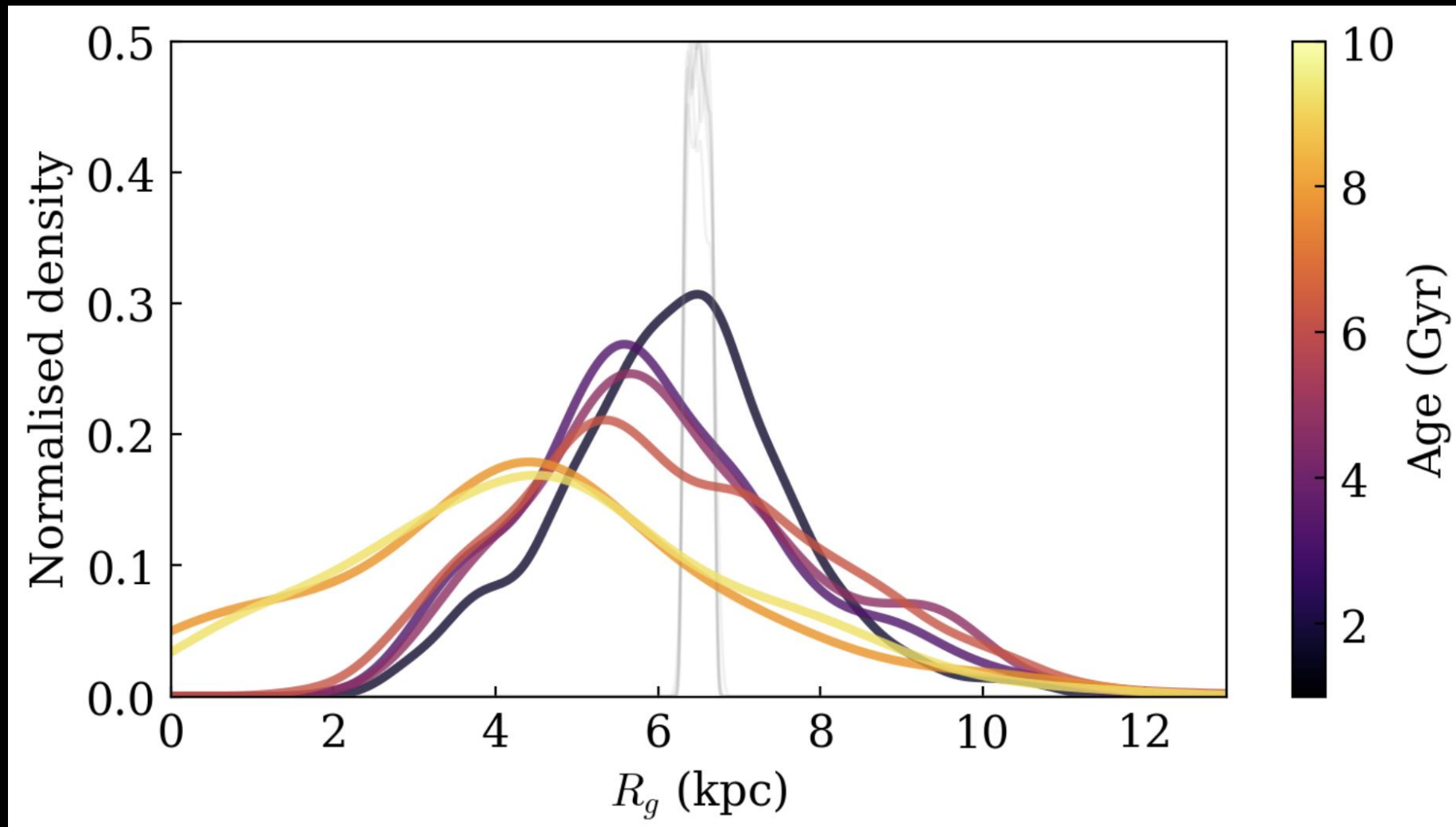
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- Bar-driven migration at the **bar-formation epoch** is also compatible with this result (Haywood+2024)



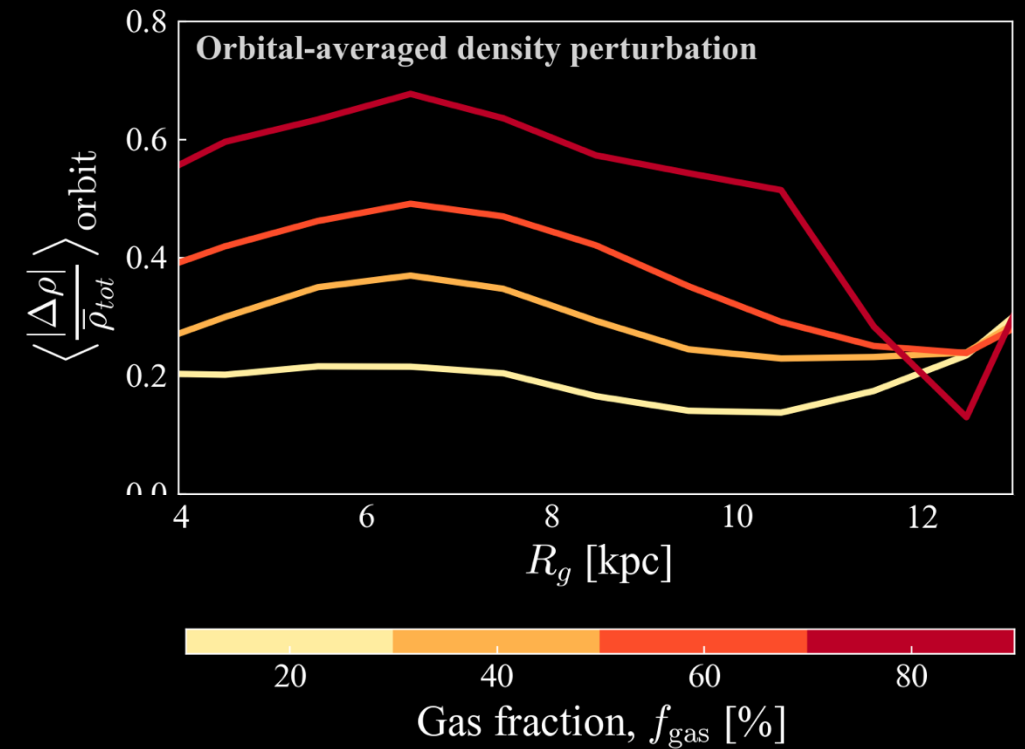
Conclusion

- **Importance of the decelerating bar** to explain the chemo-chrono-dynamical pattern of the Milky Way, e.g. age-metallicity; α -bimodality; azimuthal metallicity features
- Modelling age-metallicity-kinematics space can uncover the birth properties of the disc, e.g. ISM metallicity gradient and star-forming disc scale length
- **A transition of angular momentum diffusion coefficient** appears around the high- α , and low- α disc transition, which could hint for **a transition of the gas content in the Galaxy**
- The **low heating-to-migration ratio** highlights the importance of corotation resonances in the secular evolution of the Galactic disc, and is consistent with the gas-poor disc in the Nexus simulations



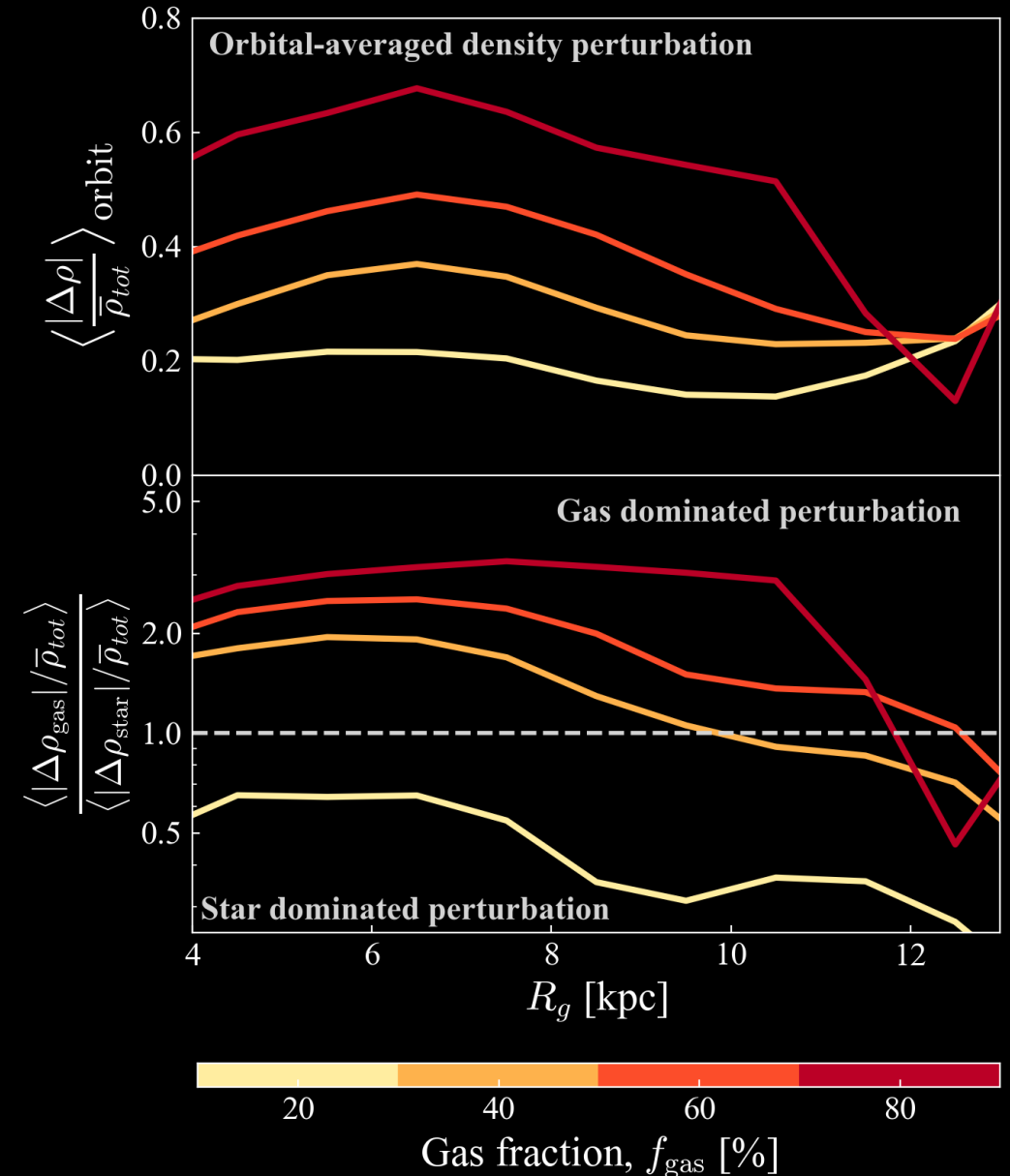
Density perturbation from gas

- Density perturbation averaged along the stellar orbits over the 1.5 Gyr

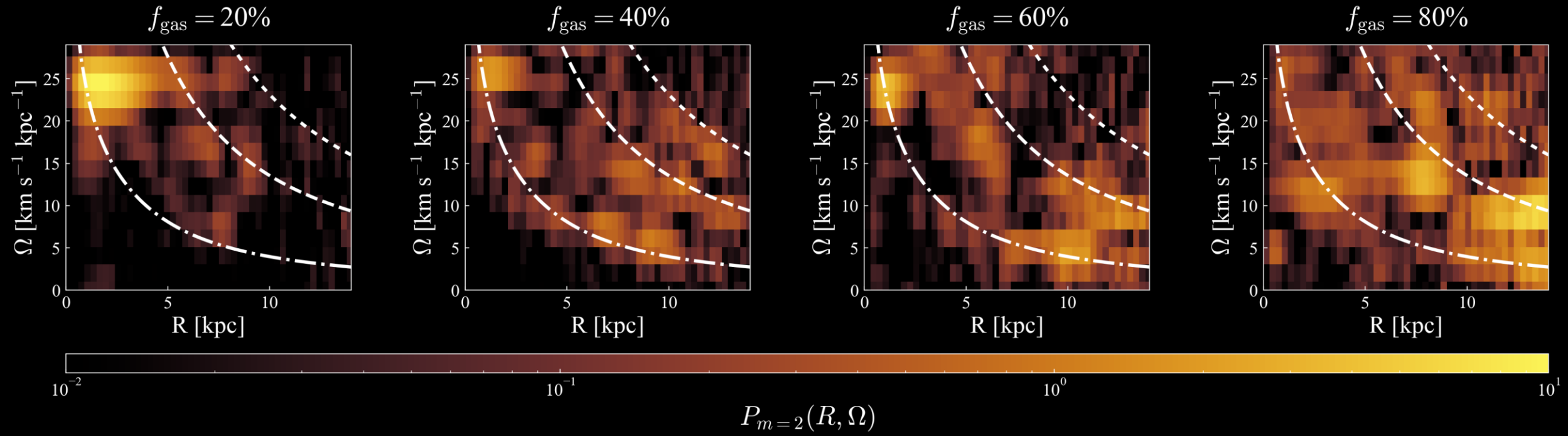


Density perturbation from gas

- Density perturbation averaged along the stellar orbits over the 1.5 Gyr
- Stars in the gas-rich disc encountered more perturbation from gas
- A transition between 20-40% where the perturbation of gas becomes more significant than the stars



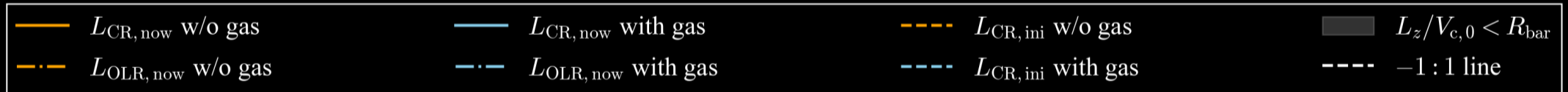
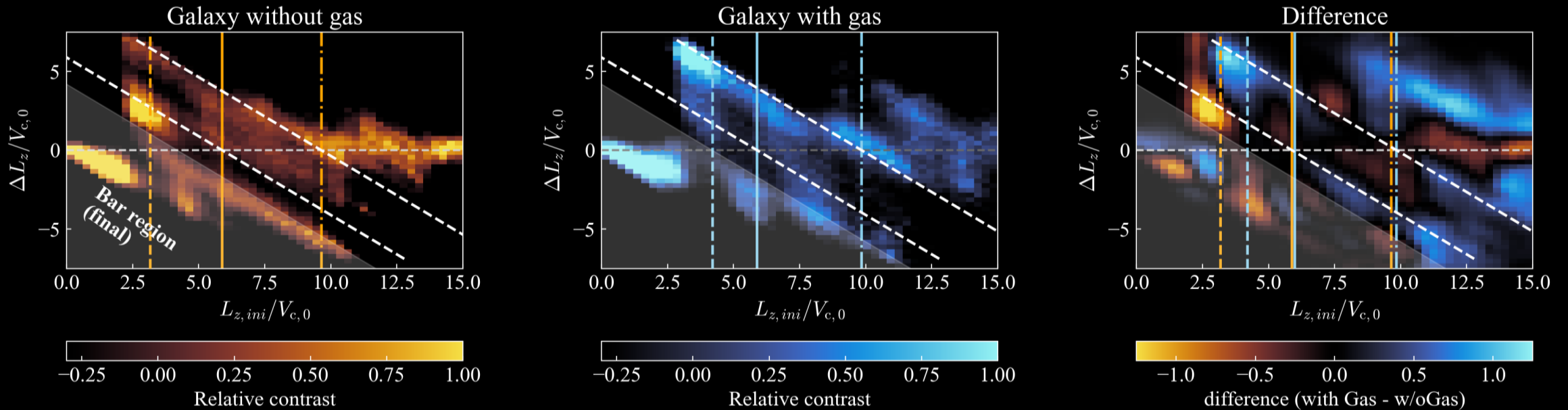
Spectrograms of m=2 mode



Impact from gas on different migration mechanisms

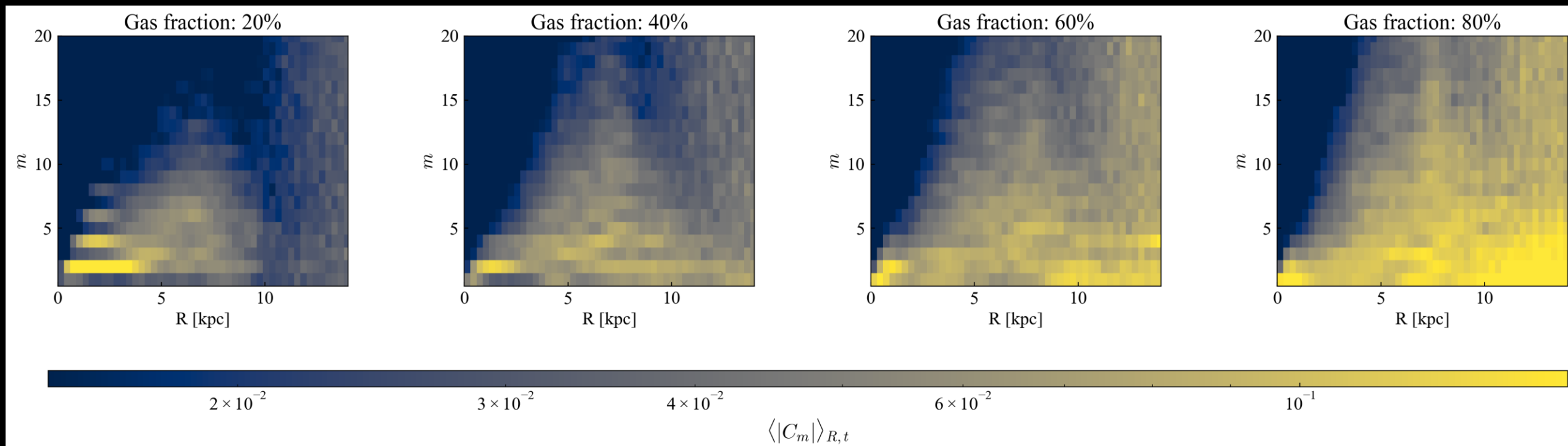
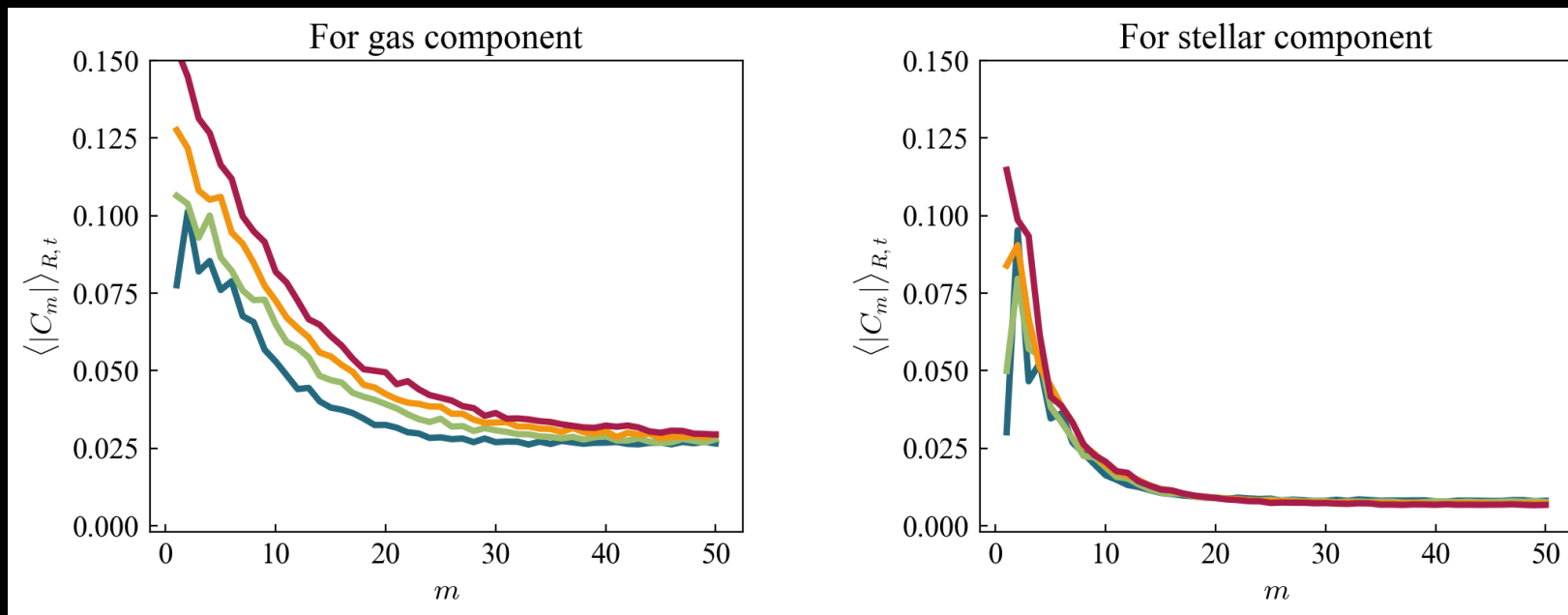
In a more gas-rich galaxy

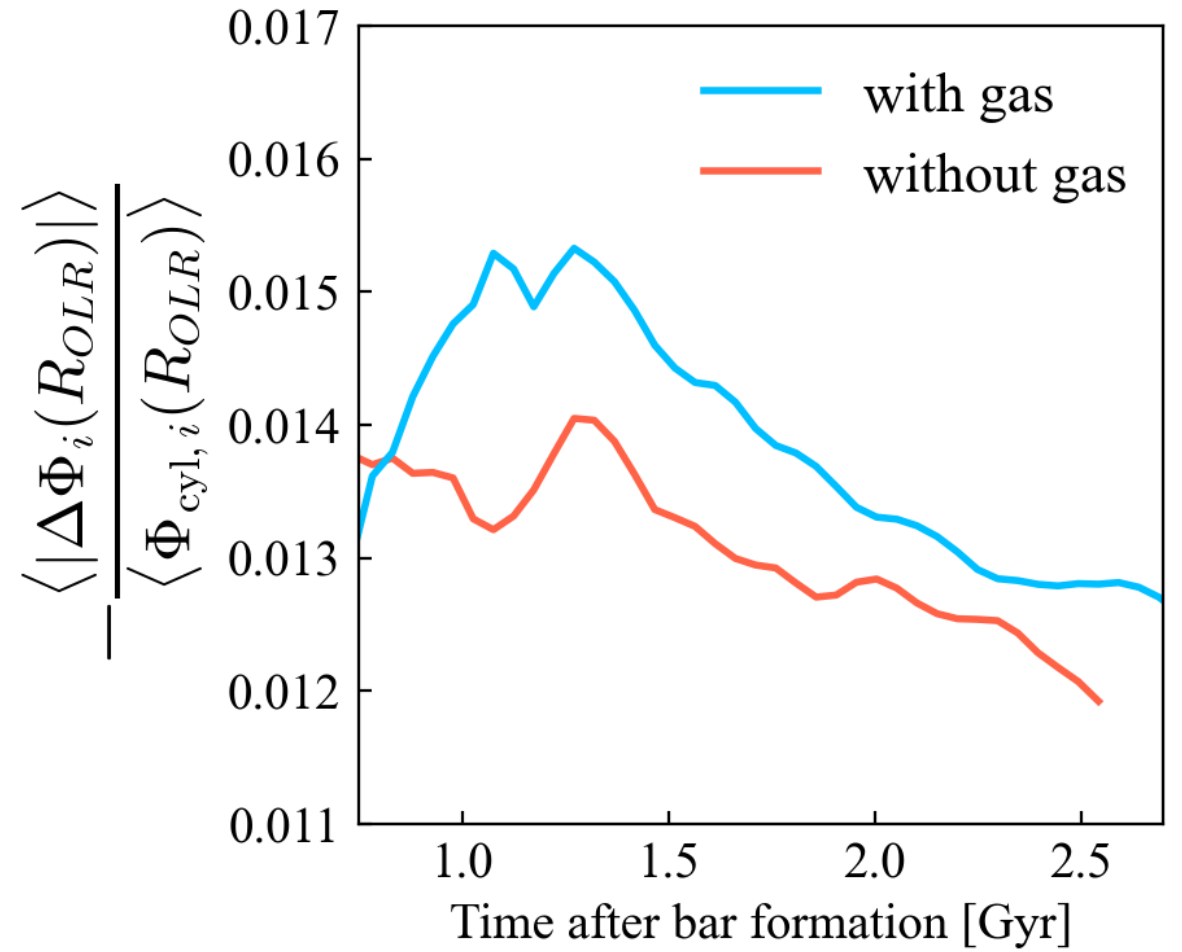
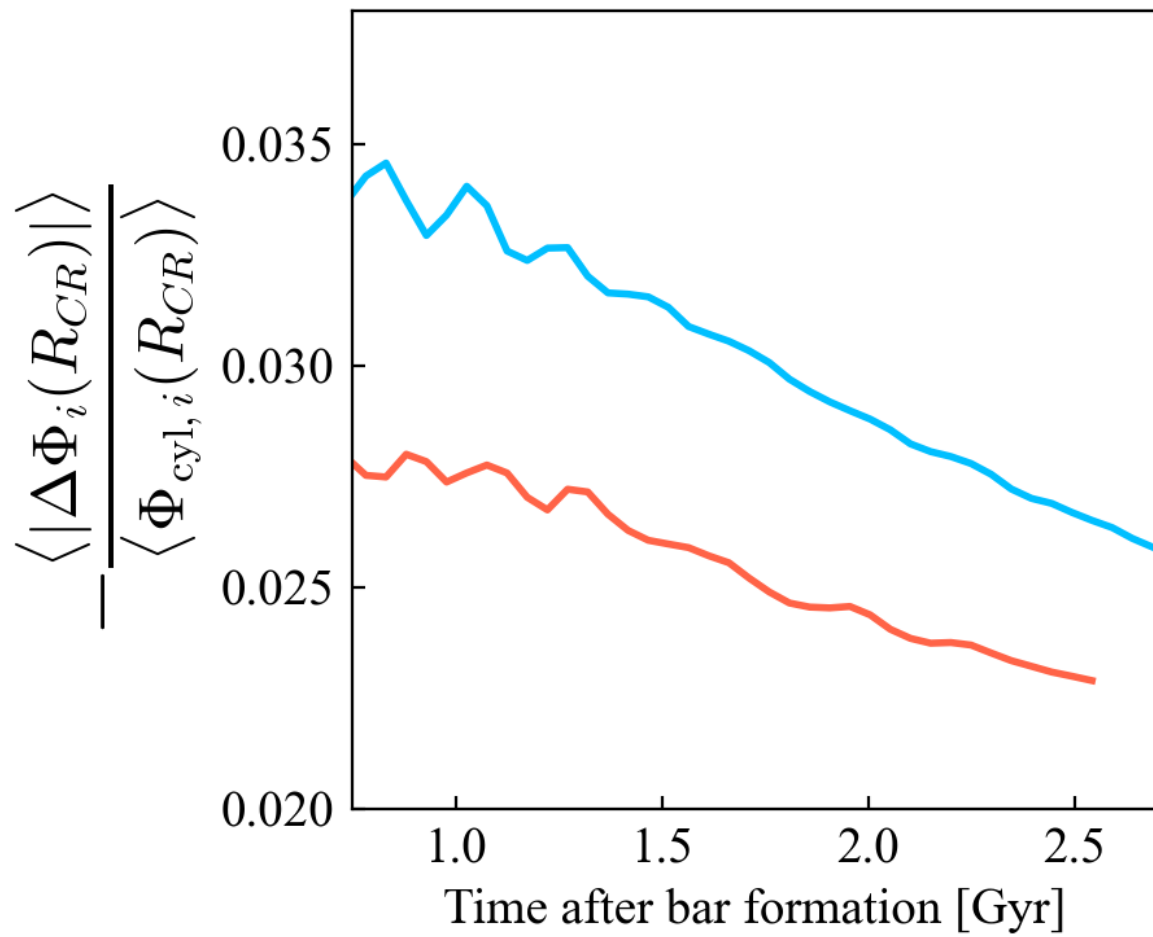
1. Less radial transportation from corotation resonance dragging
2. More outward migration to the OLR barrier
3. Also, more migration for stars outside OLR

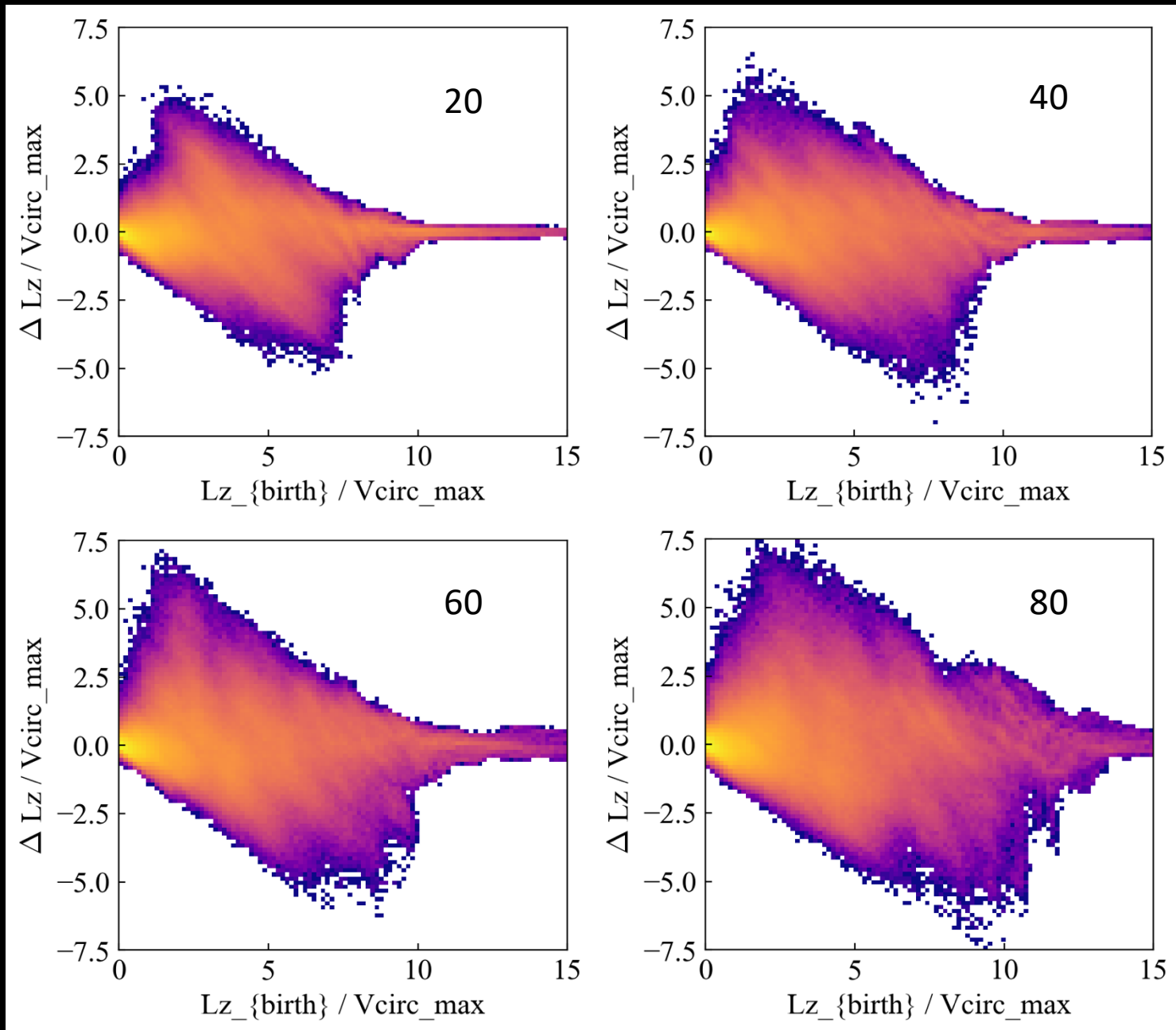


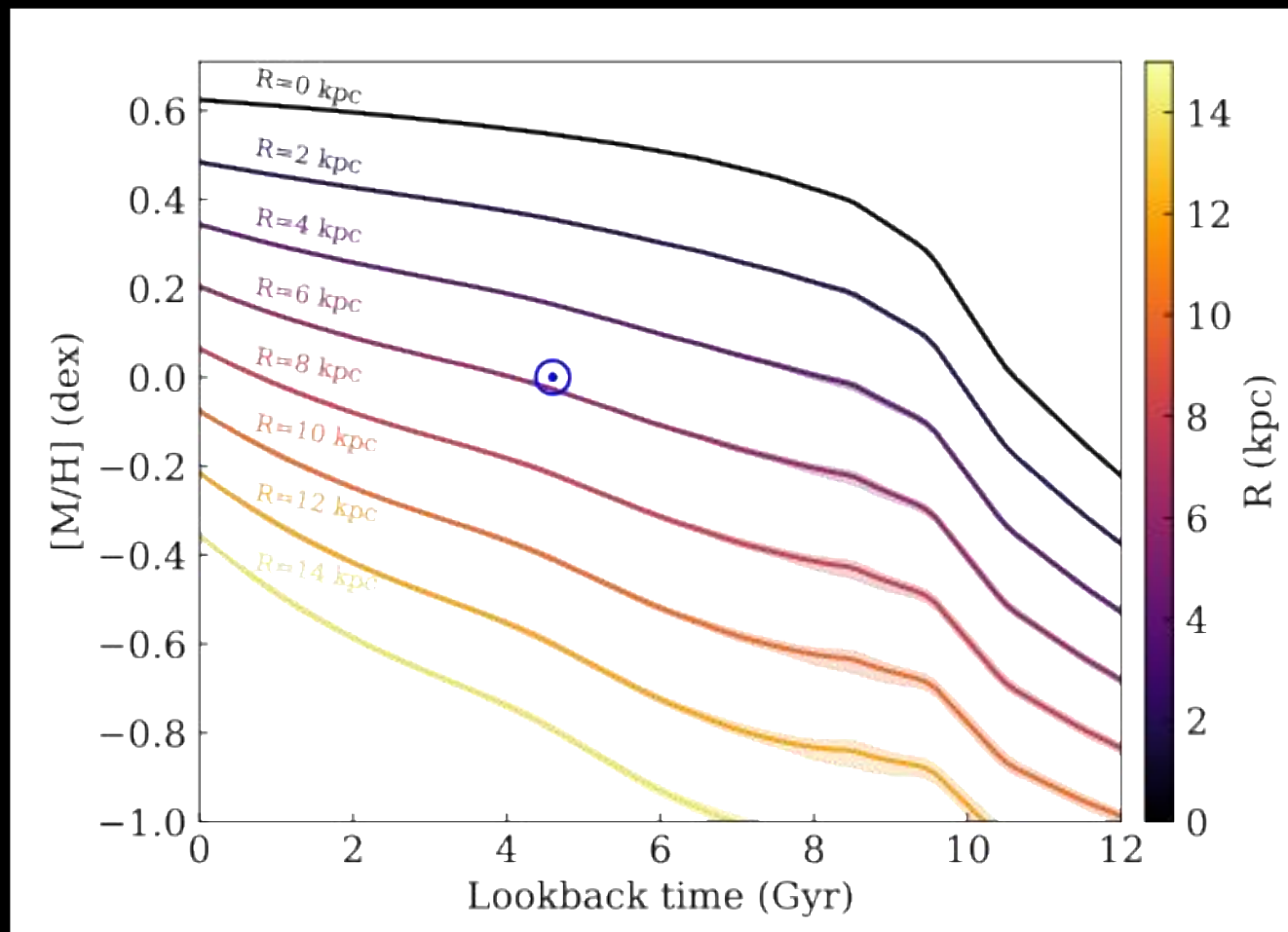
Future direction

- Secular evolution of the inner region of the Milky Way: applying the model to the reconstructed Milky Way with the orbital superposition method (Khoperskov+2025)
- Adding vertical metallicity gradient to the model, inspired by Kawata+(2018)
- Quantify the relation between the spectrogram of the galaxy with the secular evolution history and observable quantities

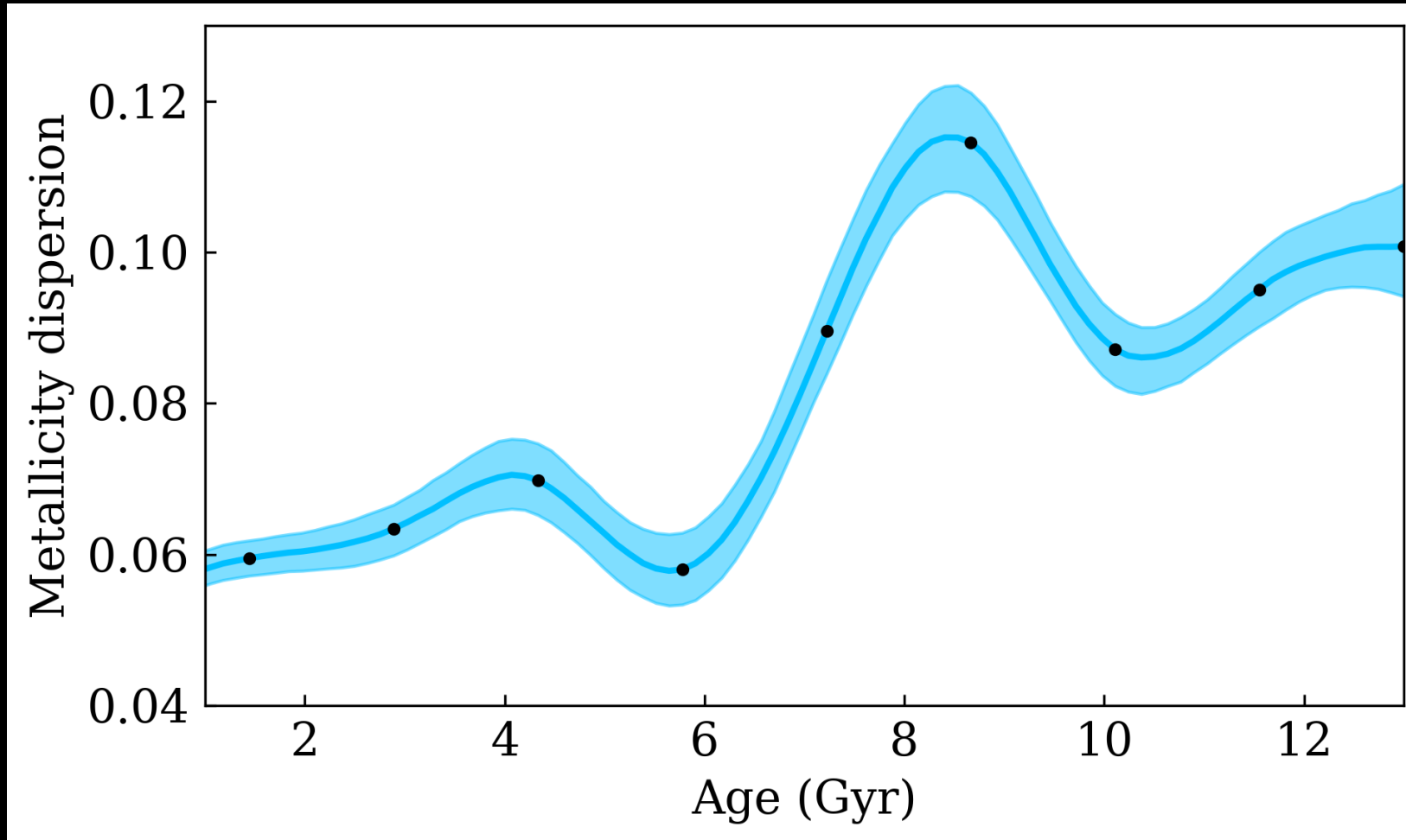


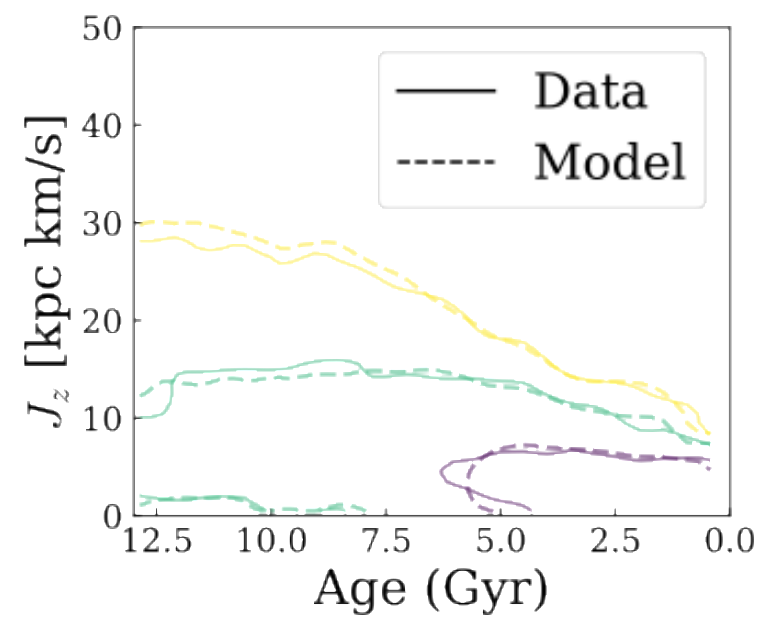
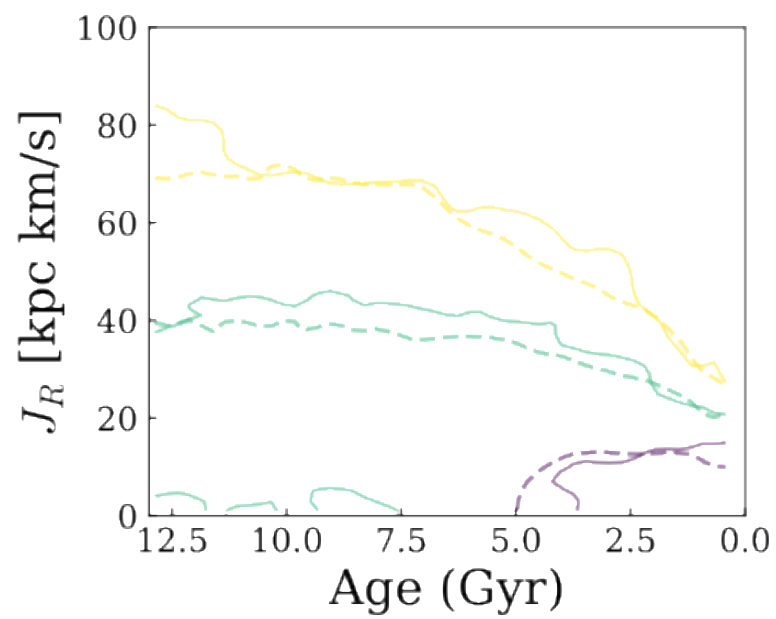
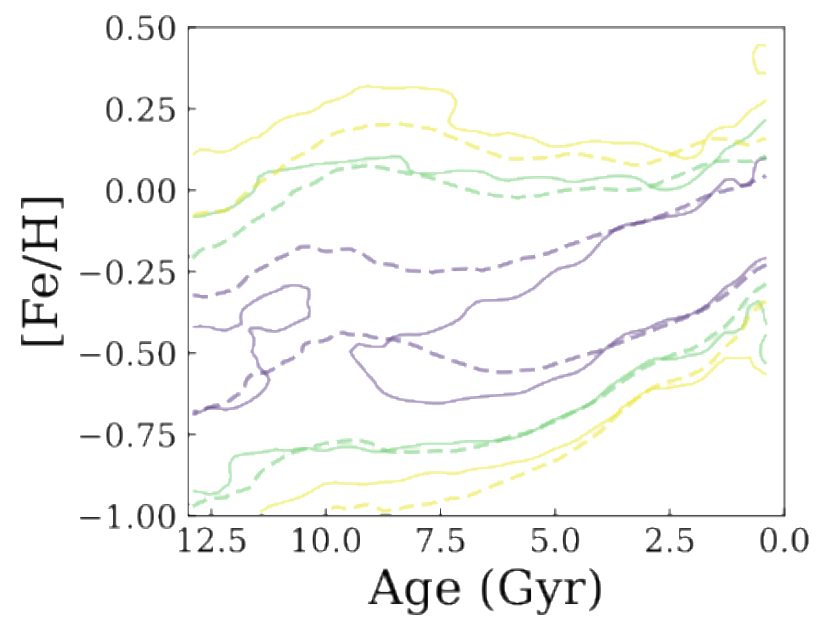


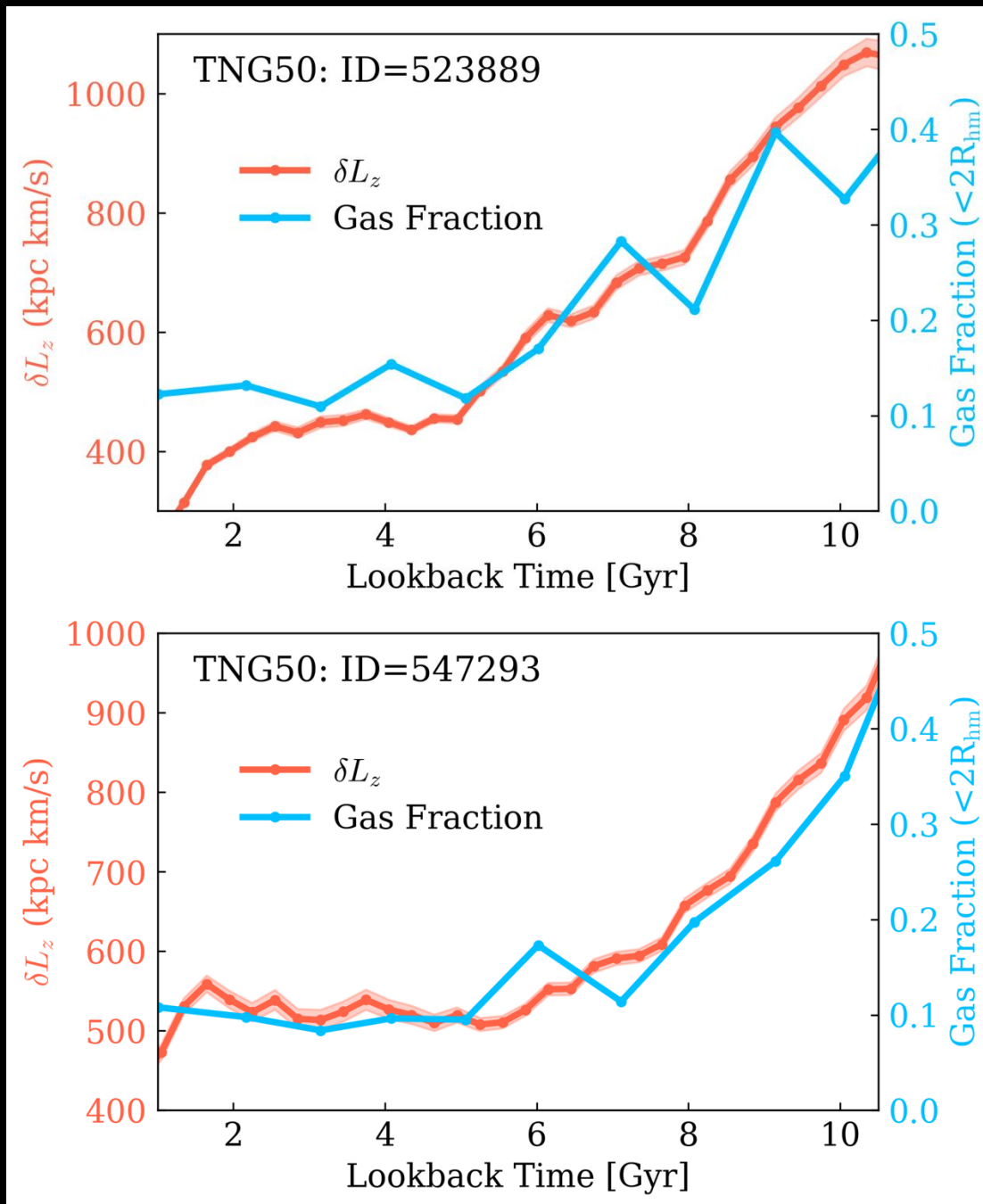


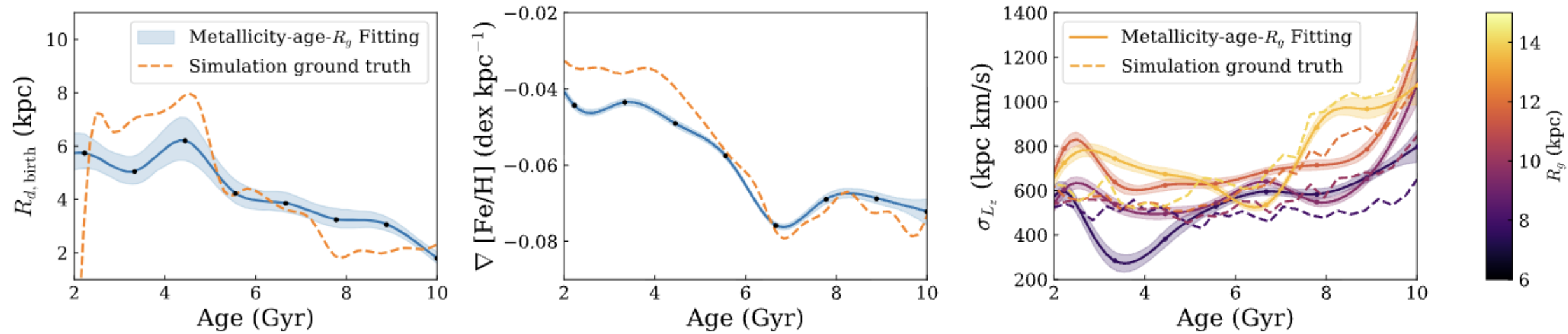


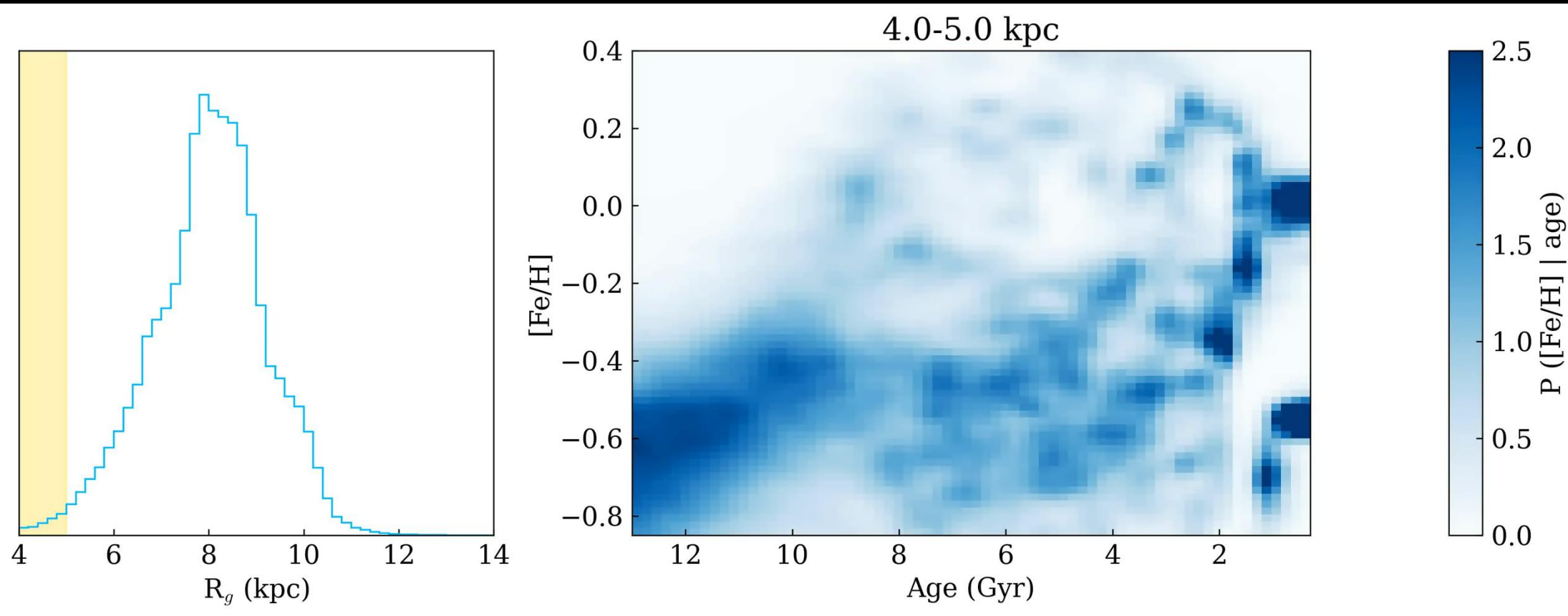
Sanity check: azimuthal metallicity dispersion





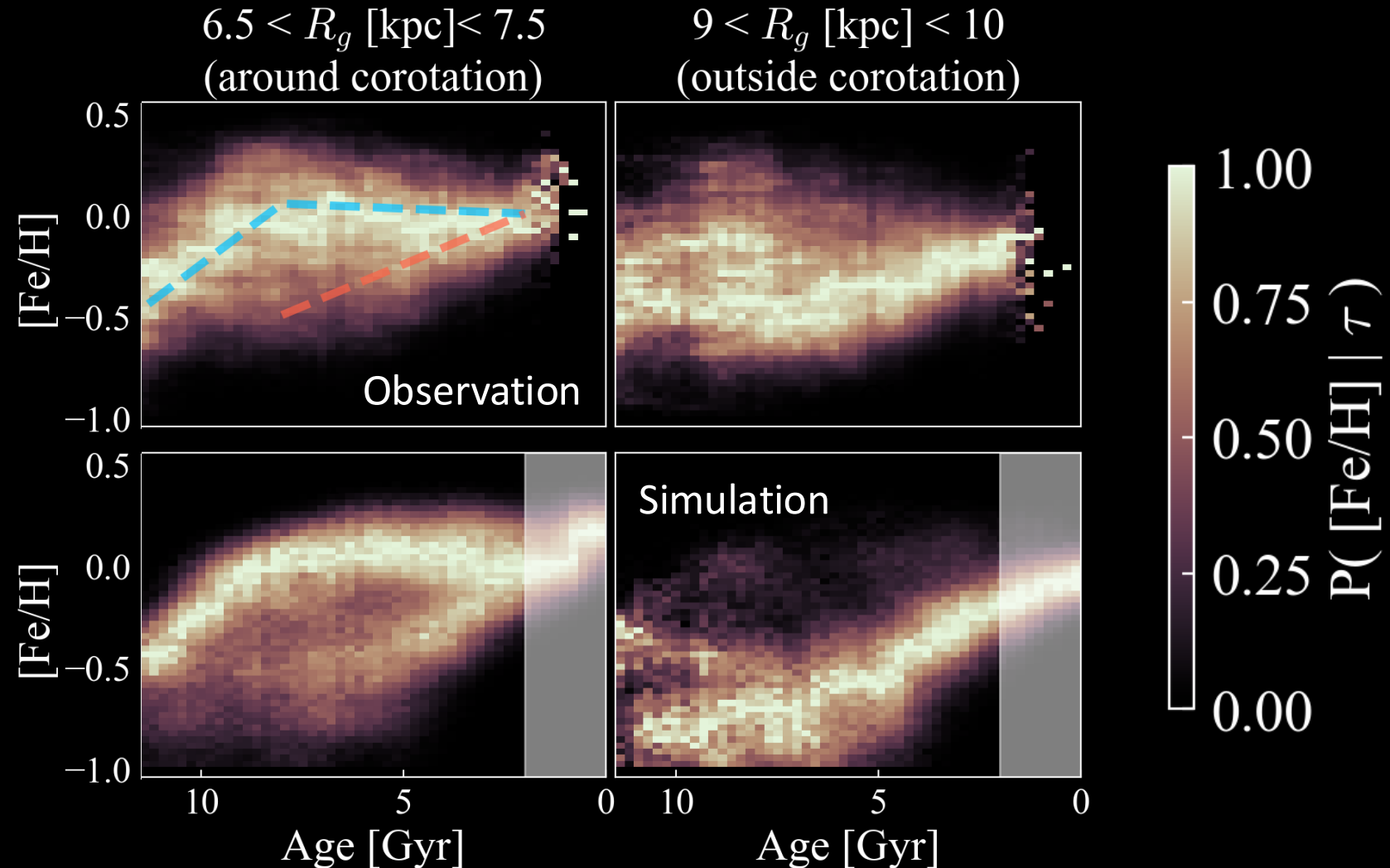






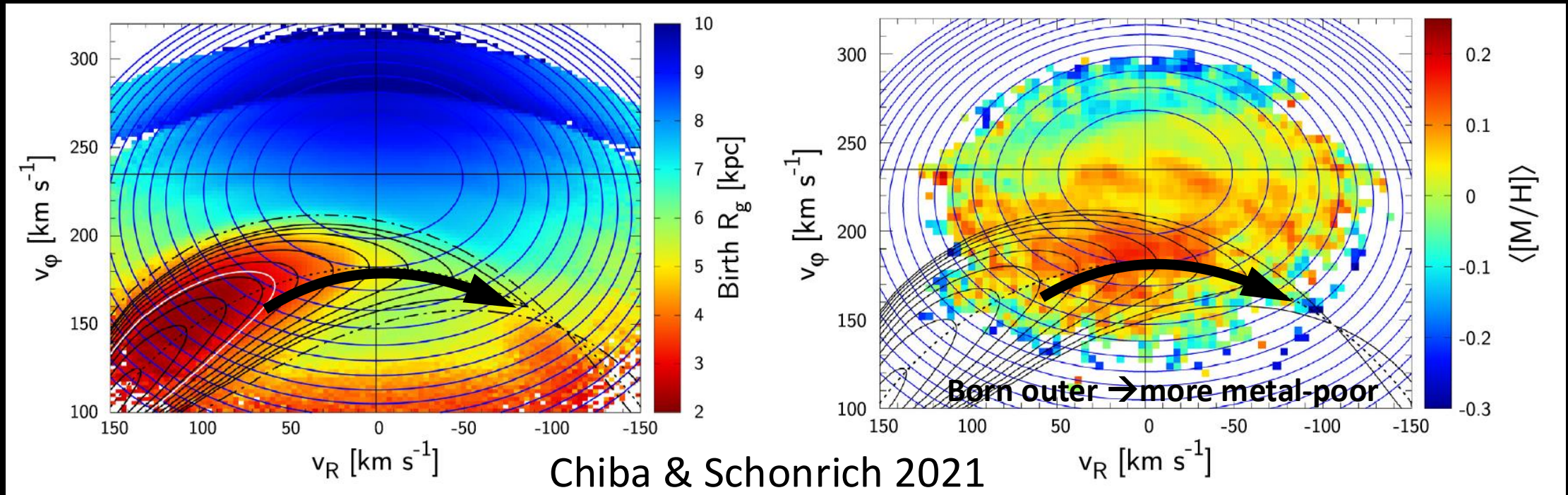
Resulting age-metallicity sequences

The guiding radii dependence



Resonant dragging of a decelerating bar

A quick introduction

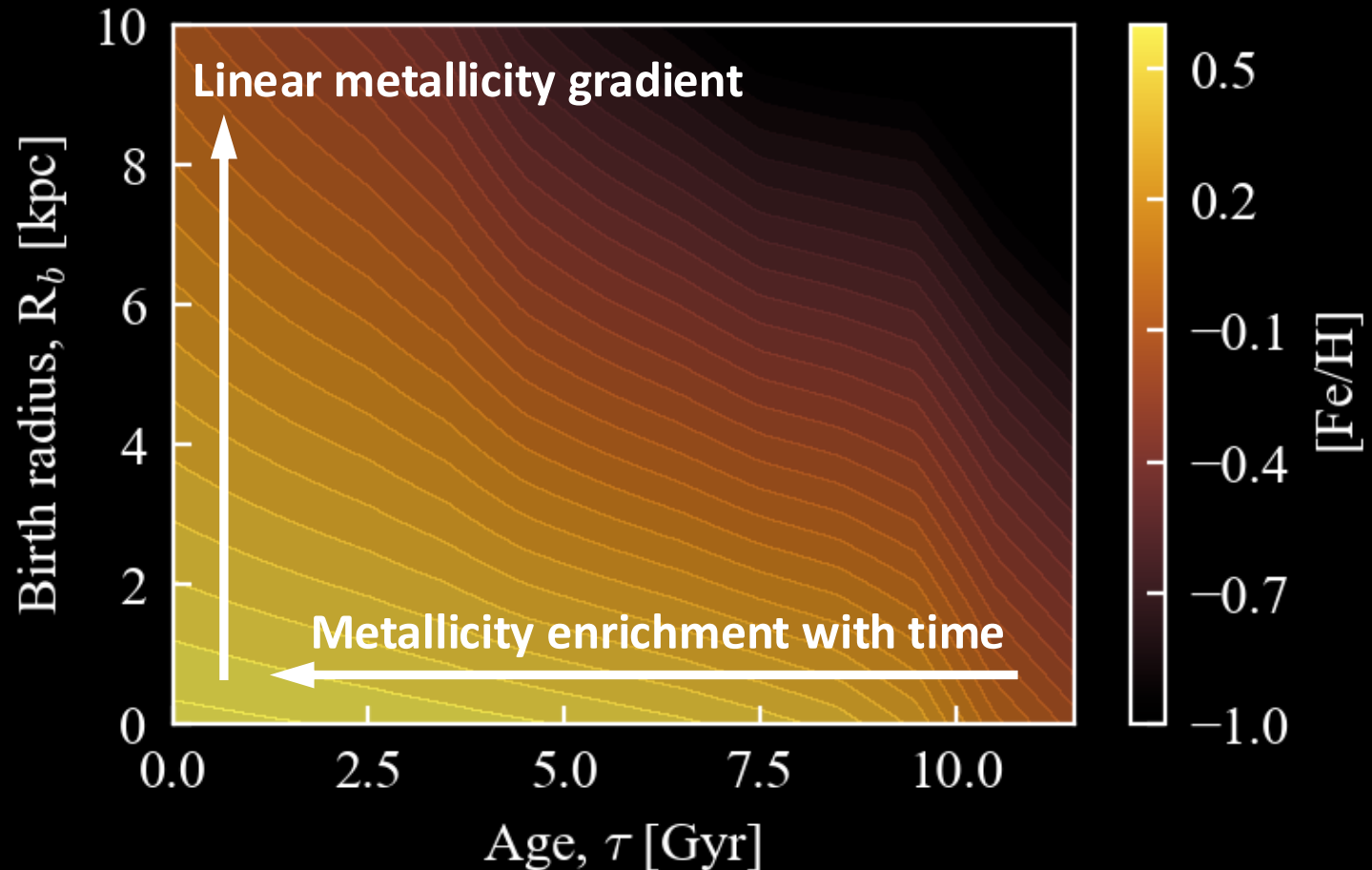


Today's bar pattern speed: $\Omega_b \sim 33 - 37$ km/s/kpc (Chiba+21; Clarke+22; Zhang+24 ; Dillamore+24, 25) → Corotation radius $R_{CR} \sim 6.2 - 7.0$ kpc

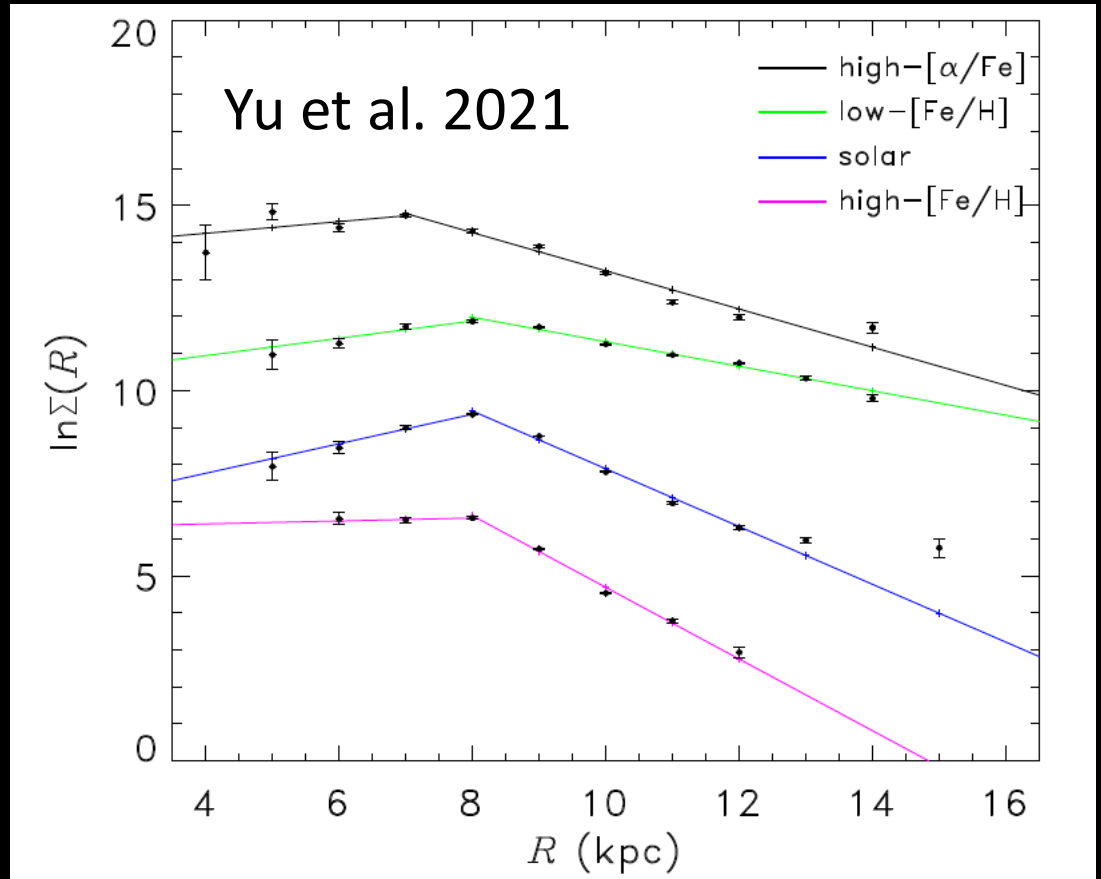
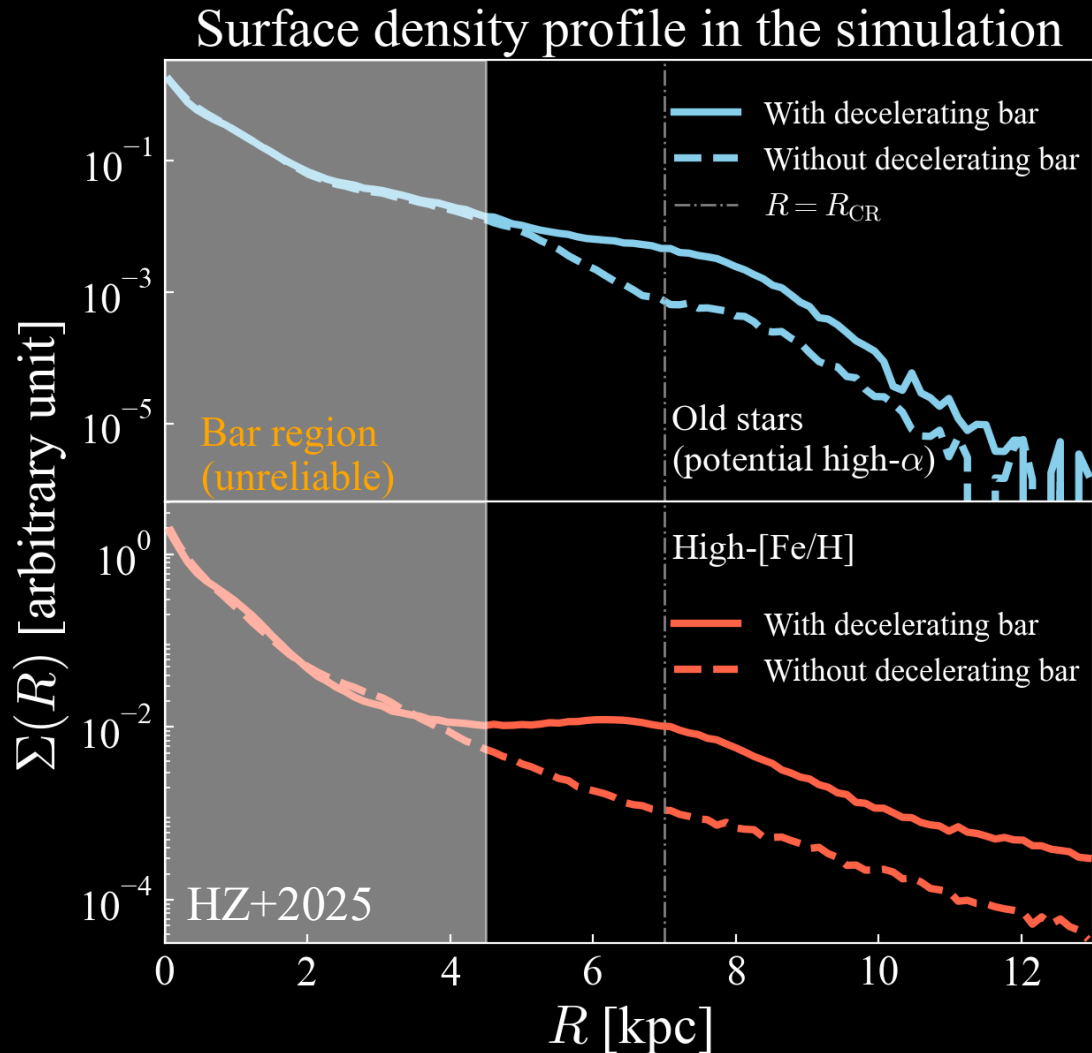
Resonant dragging of a decelerating bar

Test-particle simulation setup

This is adopted from Lu+24, which calibrated with observed Milky Way's metallicity pattern

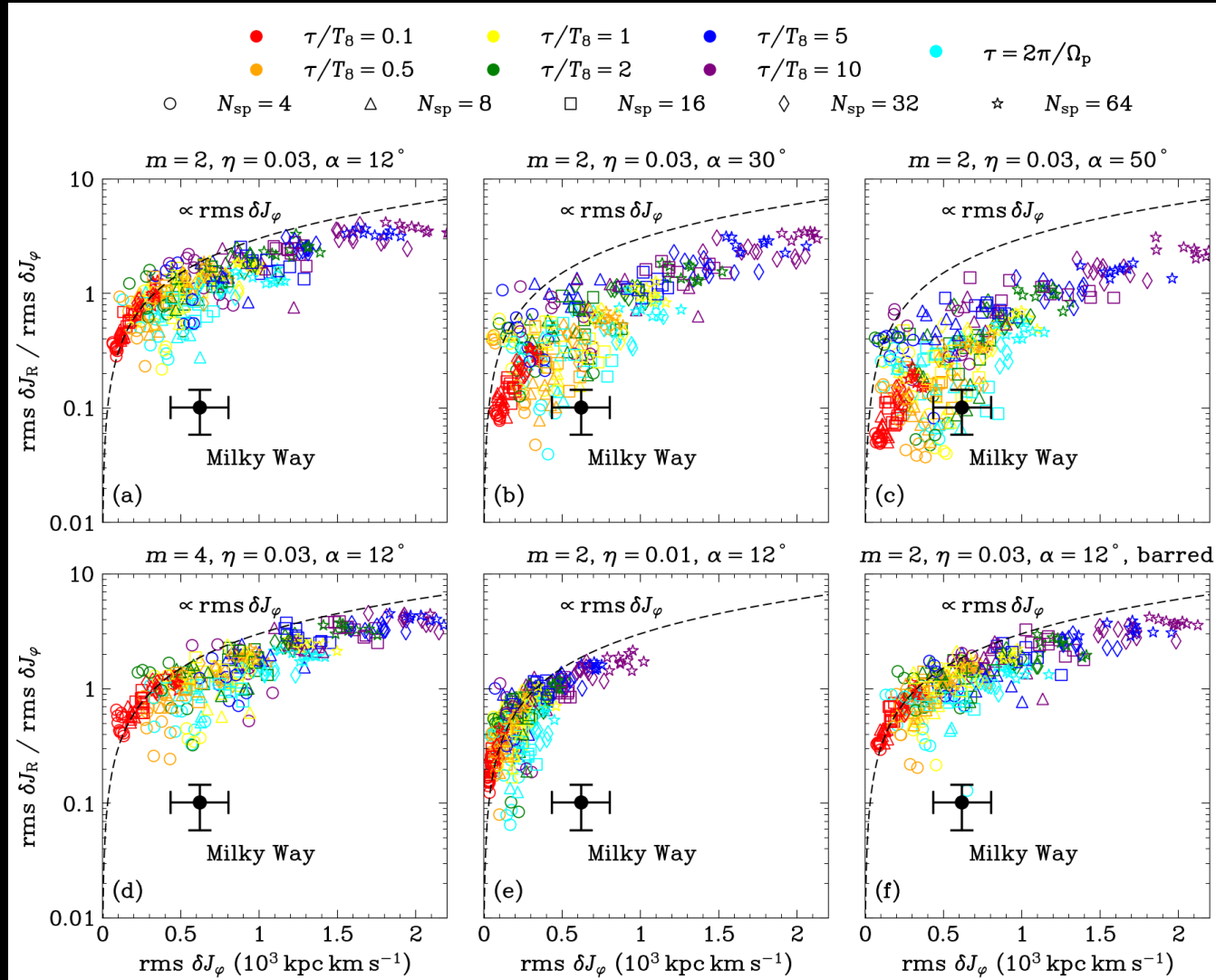


Implications: 3) Broken power-law in stellar density



See also Bovy+15, Lian+22

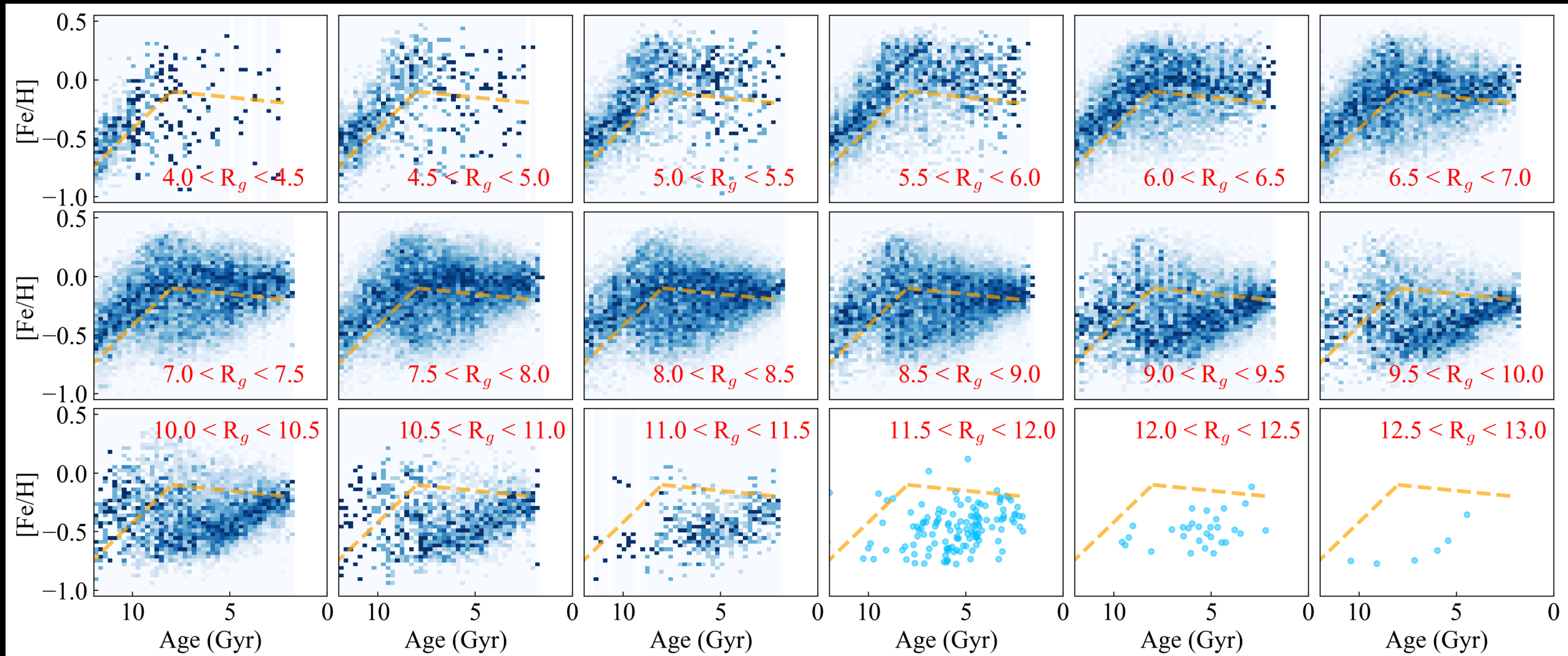
Implications: 4) Coldness of the disc

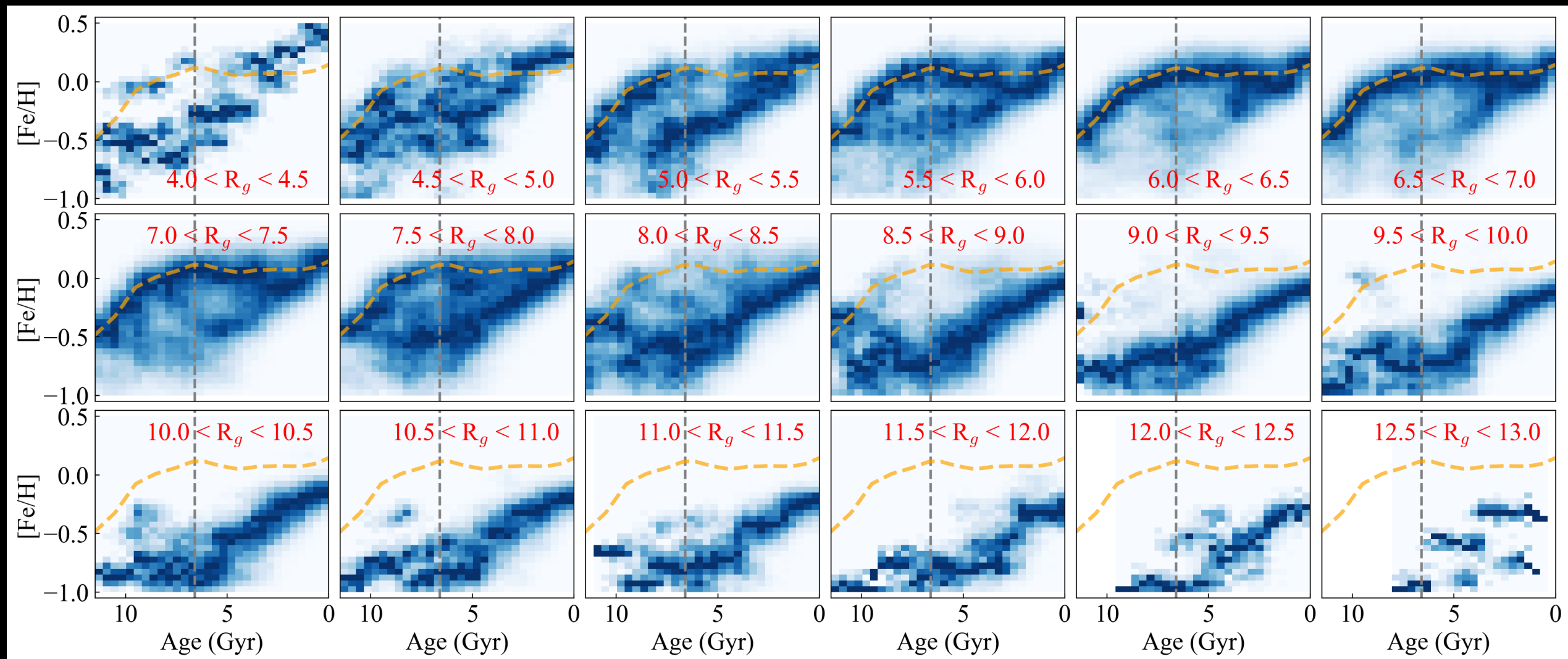


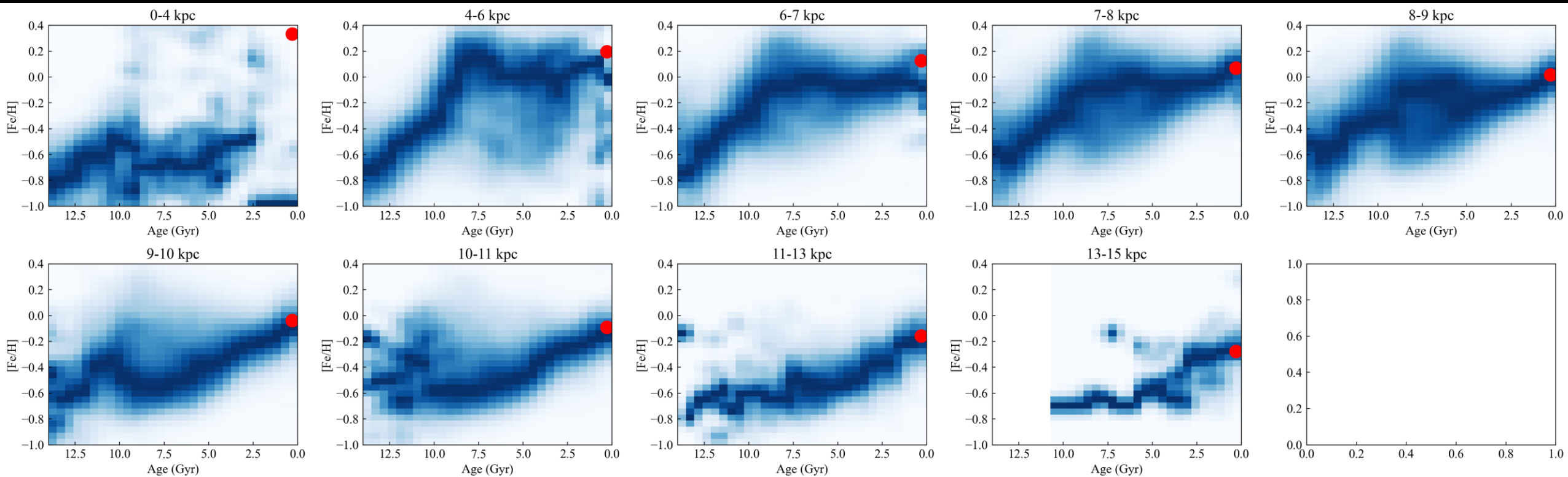
Hamilton et al. 2024

The Milky Way observation is from Frankel+20

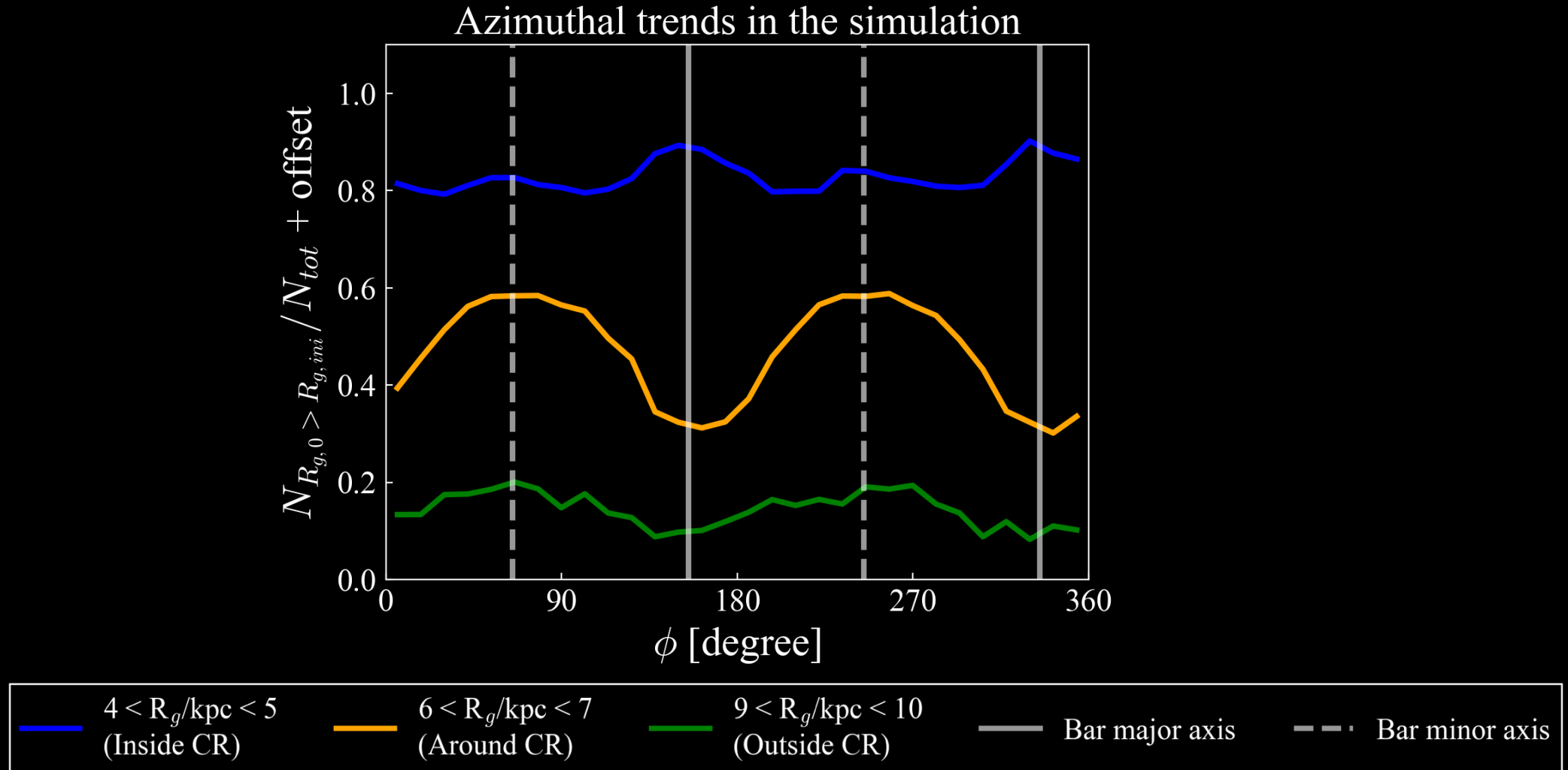
But see also the demonstration in Sellwood & Binney 2025







Implications: 2) Azimuthal patterns



Implications: 2) Azimuthal patterns

